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## Journal Article

### Author(s):

Han, Meng; Ji, Jiabao ; Balčiūnas, Tadas; Ueda, Kiyoshi; Wörner, Hans Jakob

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# 1 Attosecond circular-dichroism chronoscopy of 2 electron vortices

3 Meng Han<sup>1,\*</sup>, Jia-Bao Ji<sup>1</sup>, Tadas Balčiūnas<sup>1</sup>, Kiyoshi Ueda<sup>1,2</sup>, and Hans Jakob Wörner<sup>1</sup>

4 <sup>1</sup>Laboratorium für Physikalische Chemie, ETH Zürich, Zürich, 8093, Switzerland

5 <sup>2</sup>Department of Chemistry, Tohoku University, Sendai, 980-8578, Japan

6 \*meng.han@phys.chem.ethz.ch

## 7 ABSTRACT

Circular dichroism (CD) describes the different responses of a chiral object to circularly polarized light of opposite handedness and serves the basis of most chirality-sensitive spectroscopy techniques. All previously observed CD effects originate from the chiral sensitivity of the amplitudes of electron transitions. In contrast, CD effects in the phase of the electron transitions have barely been studied, even theoretically. Here, we present a combined experimental and theoretical investigation of the amplitude- and phase-resolved CDs of continuum-continuum  
8 transitions for electron vortices. We employ a circularly polarized attosecond pulse train to prepare electron vortices in the continuum, and a circularly polarized near-infrared laser pulse to probe the chirality of the electron vortices. Our complete experimental reconstruction of the partial-wave amplitudes and phases demonstrates that the photoionization time delay of the continuum-continuum transition depends not only on the angular-momentum quantum number  $l$  of the populated continuum state but also on its magnetic quantum number  $m$ . Our work defines a general technique called attosecond circular-dichroism chronoscopy (ACDC), which can provide new insights into electron-vortex beams, chiral molecules and magnetic materials on the most fundamental time scales.

9 Chirality is a fundamental property of asymmetric objects that are abundant in nature, ranging from spiral  
10 galaxies over human hands to chiral molecules. In a conventional view, chirality originates in the structure of  
11 objects. For example, the nuclear configuration of chiral molecules imposes the chirality onto the electronic spatial  
12 distribution, which results in chiral light-molecule interactions. Electron vortices<sup>1</sup> (also called electron ring currents  
13 in the case of bound states) are a paradigmatic example of a class of objects for which the chirality originates  
14 from their phase structure. Due to the quantization of angular momentum, a freely moving or bound electron may  
15 have a nonzero projection of its orbital angular momentum on the quantization axis. This nonzero longitudinal  
16 angular momentum  $m\hbar$  dictates the electronic helical phase  $e^{im\phi}$  spiralling about the quantization axis, where  $m$   
17 is the magnetic quantum number and  $\phi$  is the azimuthal angle. Such an electron vortex or electron ring current  
18 has naturally attracted much interest<sup>2-10</sup> due to its chiral phase structure. For example, an unusual kind of Ramsey  
19 interference between photoelectron wave packets produced by a pair of time-delayed, counter-rotating circularly  
20 polarized, attosecond pulses was investigated theoretically<sup>2,3</sup> and then confirmed experimentally<sup>4,5</sup> in multiphoton  
21 ionization regime using visible light pulses. The electron vortices have also been exploited in electron-energy-loss  
22 spectroscopy of magnetic materials<sup>11</sup> and the electronic spin polarization from atoms<sup>12</sup>. Although the Ramsey  
23 interference between electron vortices can probe their helical phases, their attosecond chiral dynamics interacting  
24 with lights have so far escaped scrutiny in experiments as a consequence of the shortage of circularly polarized  
25 attosecond extreme-ultraviolet (XUV) pulses<sup>13-16</sup> and suitable attosecond metrology in circular polarization.

26 Chiral recognition of molecules is an important topic in biochemical science, and most of the related techniques  
27 are based on the interactions with circularly polarized light (CPL). For example, in traditional CD spectroscopy  
28 of chiral molecules, the asymmetry in the absorption of right versus left CPL is typically less than  $10^{-3}$ , since it  
29 is dictated by magnetic-dipole transitions. Recently, several techniques of higher selectivity based on the intense  
30 electric-dipole transitions have been developed, such as laser-induced mass spectrometry<sup>17</sup>, Coulomb-explosion  
31 imaging<sup>18,19</sup>, photoelectron circular dichroism<sup>20,21</sup> and high-order harmonic spectroscopy<sup>22,23</sup>. Some of them can  
32 increase the CD signal beyond 10%. However, all of these chiroptical techniques are based on the amplitude of real-  
33 valued electronic-transition dipoles, such that possible CDs in the transition phase have not been considered. With  
34 the development of ultrafast science into the attosecond domain<sup>24</sup>, the phase information of electronic transitions has  
35 become accessible by attosecond metrology, including the attosecond streak camera<sup>25,26</sup> and the reconstruction of  
36 attosecond beating by interference of two-photon transitions<sup>27-29</sup> (RABBIT). After determining both the amplitude  
37 and the phase of electronic transitions, it can be regarded as a “complete” measurement.

38 In a recent advance, we established attosecond metrology in circular polarization and demonstrated a plug-in

39 apparatus to simplify the generation of CPL attosecond XUV pulses based on the non-collinear high-order harmonic  
40 generation (HHG) process<sup>15,16</sup>. Here, we employ this metrology to study and manipulate the chiral dynamics of  
41 electron vortices on attosecond time scales. A circularly polarized attosecond pulse train is used to photoionize argon  
42 atoms, preparing electron vortices with well-defined helicity in the continuum state. We then probe the electron  
43 vortices with a synchronized co-rotating or counter-rotating near-infrared (IR) laser pulse through circular-RABBIT  
44 measurements. We observe that the sideband (SB) yield in the co-rotating geometry is remarkably enhanced  
45 compared with that in the counter-rotating case with a CD signal ranging up to 35%. More importantly, when  
46 switching the helicity of the IR probe, we demonstrate that the phase of the SB photoelectrons has dichroic structures  
47 and opposite bending directions along the photoemission angle with respect to the light propagation direction, and the  
48 corresponding two-photon (XUV+IR) photoionization time delays can differ by several hundreds of attoseconds. Our  
49 findings are supported by solving the time-dependent Schrödinger equation (TDSE) in three dimensions. The insights  
50 gained from the calculation are then used to retrieve a complete set of partial-wave amplitudes and phases from the  
51 experimental data, enabling to separate the phase into the bound-continuum and continuum-continuum transitions  
52 and then extract the CD of the continuum-continuum transition phases. Our study provides a quantum-mechanically  
53 complete description of the photoionization and continuum dynamics.

54 In our experiments, the circularly polarized attosecond XUV pulses were generated through HHG in xenon atoms  
55 driven by two non-collinear counter-rotating circularly polarized IR (800 nm) beams using a compact beam-in-beam  
56 setup. The XUV spectrum contained the odd-order harmonics from H9 (13.95 eV) to H15 (23.25 eV). The weak  
57 probing IR field was tuned to be circularly polarized with the same or the opposite helicities with respect to that of  
58 XUV. The XUV and IR pulses were spatiotemporally overlapped and then focused onto a thin supersonic beam of  
59 argon, and the three-dimensional momenta of the ionized electrons and ions were measured in coincidence using  
60 a COLTRIMS (Cold target recoil ion momentum spectroscopy) spectrometer<sup>30,31</sup>. The XUV-IR phase delay was  
61 actively stabilized during measurements with a continuous-wave (cw) HeNe laser to a temporal stability of better  
62 than 30 as<sup>32</sup>. Our experimental setup is illustrated in the extended-data Figure 5 and more details are given in the  
63 Methods section.

64 Figure 1a illustrates the coordinate system used throughout this work, in which the light co-polarization plane is  
65 the x-y plane and the light propagation direction defines the z axis. The outermost valence shell of argon atoms is 3p  
66 which consists of three degenerate orbitals, i.e.,  $p_+$  (left helicity),  $p_-$  (right helicity) and  $p_0$ , where the quantization  
67 axis of the atomic orbitals is the z axis. Note that in previous RABBIT experiments with linearly polarized lights  
68 the quantization axis is usually chosen to be the polarization direction. Our left circularly polarized XUV field will

69 preferentially ionize the co-rotating orbital, i.e., the  $p_+$ , forming an electron-vortex continuum state with  $m = 2$ . In  
70 the extended-data Fig. 6, we show the calculated ionization cross sections and the photoelectron angular distributions  
71 from the degenerate 3p orbitals, which confirms the dominance of ionization from  $p_+$ . In the light polarization plane,  
72 the photoelectron momentum distributions are isotropic and form a doughnut shape due to the circular polarization of  
73 both light fields. Since the net angular momentum direction of the electron vortices and the spin angular momentum  
74 direction of the probe light are both along the z axis, the chirality must manifest itself in the  $\theta$ -resolved photoelectron  
75 angular distribution, where  $\theta$  is the photoelectron emission angle with respect to the light propagation direction.

76 Figures 1b-d show the measured angle-resolved photoelectron energy spectra in the XUV-only, co-rotating, and  
77 counter-rotating cases, respectively. The photoelectron emission angle in the polarization plane  $\phi = \arctan(p_y/p_x)$   
78 was integrated over its  $2\pi$  range and the XUV-IR delay was integrated over two IR optical-cycle periods. We  
79 observe three main peaks of the electron vortices corresponding to the photoionization by H11, H13 and H15 in the  
80 XUV-only case, and two sidebands (SB12 and SB14) after introducing the probe light. The sidebands are formed by  
81 the interference between the electronic wavepacket that absorbed one IR photon from the lower main peak and that  
82 released one IR photon from the higher main peak. Our experiment shows that the SB yield is remarkably enhanced  
83 in the co-rotating case compared to the counter-rotating case, which directly manifests the CD effect on the amplitude  
84 of the continuum-continuum transitions of the electron vortices. In Fig. 1e, we illustrate the photoelectron-energy  
85 and CD spectra at the angle of  $90^\circ$ , i.e., the co-polarization plane, which has the highest counts and experimental  
86 resolution. The energy-dependent CD is defined as  $[Y_{\text{co}}(E_k) - Y_{\text{counter}}(E_k)]/[Y_{\text{co}}(E_k) + Y_{\text{counter}}(E_k)]$ , where  $Y_{\text{co}}(E_k)$   
87 and  $Y_{\text{counter}}(E_k)$  are the normalized photoelectron counts in the co- and counter-rotating cases, respectively. Our  
88 experimental result demonstrates that the CD signals of SB12 and SB14 can reach up to 35% and 30%, respectively,  
89 which is arguably a huge CD signal compared to the previous chiroptical methods. Note that the CD signal is negative  
90 at the main peaks because of the depletion effect of the continuum-continuum transitions. Our experiment reveals a  
91 basic rule in the electron-photon chiral interaction that the electron vortex prefers to absorb or release a co-rotating  
92 photon, which is opposite to a previous experimental observation<sup>33</sup> where the sideband in the counter-rotating  
93 configuration was reported to be dominant. In the Methods section, we provide an analytical perspective of the  
94 amplitude CD to support our conclusion.

95 When varying the XUV-IR delay, the angle-resolved sideband yield oscillates with a period of  $2\omega$  ( $\omega$  is the  
96 IR center frequency) due to the pathway interference, and the phase of the yield oscillation (also called RABBIT  
97 phase) contains the attochirp of the XUV field and the phases of electronic two-step transitions in the ionization  
98 process. Here we focus on the angle-resolved RABBIT phase within one sideband and therefore the XUV attochirp

99 which only depends on the photon energy can be ruled out. In Figs. 1f-g, we show the delay-resolved photoelectron  
100 angular distributions of SB12 in co- and counter-rotating geometries, respectively, where the photoelectron energy is  
101 integrated over [2.4, 3.2] eV and the photoelectron emission angle in the polarization plane  $\phi$  is fixed at  $90^\circ$ . Our  
102 experimental result illustrates the fact that the photoelectrons emitted along different angles with respect to the light  
103 propagation direction show different phases for the yield oscillation. Performing Fourier transformation along the  
104 axis of the XUV-IR delay, we extract the angle-dependent RABBIT phases for the two geometries, as illustrated in  
105 Fig. 1h, and for clarity we add these RABBIT-phase curves onto the two-dimensional RABBIT trace plots in Figs.  
106 1f-g with dashed lines. The RABBIT phase displays the opposite bending directions for the two geometries. For  
107 the co-rotating geometry, the photoelectrons emitted closer to the light propagation direction are delayed in time.  
108 In contrast, for the counter-rotating geometry the photoelectrons emitted close to  $0^\circ$  or  $180^\circ$  are mostly advanced  
109 temporally compared to those emitted in the light-polarization plane. More importantly, by simply switching the  
110 IR helicity, the photoionization time delay of the continuum-continuum transition can be tuned on the attosecond  
111 timescale. For the photoelectrons emitted in the light polarization plane, the CD effect on the photoionization time  
112 delay is about 100 as and it increases to several hundreds of attoseconds for the photoelectrons emitted along the  
113 light propagation direction.

114 To validate our findings, we resort to solving the three-dimensional (3D) TDSE<sup>34</sup> using an effective potential for  
115 argon. In the calculation, we considered the three 3p orbitals [ $p_+$  (left helicity),  $p_-$  (right helicity) and  $p_0$ ]. The  
116 calculations confirmed that the ionization from  $p_+$  contributes 70% of the total cross section, largely exceeding those  
117 from the other two orbitals. More details about the TDSE simulations are given in the Methods section. In Figs.  
118 2a-b we illustrate the simulated delay-integrated angle-resolved photoelectron spectra for the two geometries, and in  
119 Fig. 2c we show the photoelectron-energy and the corresponding CD spectra in the light-polarization plane. Note  
120 that these results are averaged over the three 3p orbitals. The TDSE simulation predicts that the CD signal could  
121 reach 43% for SB12 and 30% for SB14, which agrees with our observations in a reasonable range considering the  
122 assumptions made in the TSDE calculations, e.g. the equal intensities for each harmonic order. The angle-resolved  
123 RABBIT traces of SB12 in the two geometries and the extracted RABBIT phases are illustrated in Figs. 2d-f,  
124 respectively. It is clear that these two kinds of probes cause the opposite bending directions for the phase of the  
125 emitted photoelectrons, and the bending degree of the phase in the counter-rotating case is larger than that in the  
126 co-rotating case. These orbital-averaged results qualitatively agree with our experiment.

127 In Figs. 2g-i, we illustrate the corresponding simulation results from the dominant orbital, i.e.,  $p_+$ . The basic  
128 structures of the RABBIT phases are not changed but their curvatures are obviously increased. In the counter-rotating

129 case, there is a  $\pi$ -shift between the emissions in the polarization plane and along the light propagation direction,  
130 which gives rise to the relatively larger bending of the counter-rotating phase in the orbital-averaged result. In the  
131 extended-data Fig. 7, we illustrate the RABBIT traces from  $p_-$  and  $p_0$  orbitals in the two geometries. There is no  
132 CD effect for the ionization from the  $p_-$  orbital, since the accessed electronic continuum has  $m = 0$ , i.e. no chirality.  
133 Ionization from the  $p_0$  orbital has similar CD effects in the sideband yield and phase, but the CD degree is smaller  
134 compared to the case of  $p_+$  due to the smaller  $m$ -value of the electron vortices. The sensitivity of the phase CD to  
135 the properties of the initial state demonstrates that our ACDC technique is a sensitive probe of the orbital structure  
136 of the ionized target. This conclusion is additionally confirmed by the calculated ACDC effect in He, shown in  
137 extended-data Fig. 8.

138 Figure 3a and c show energy-level diagrams based on ionization from the  $p_+$  ground-state orbital that rationalize  
139 the experimental observations on different RABBIT phases for the two different probes. The atomic eigenstates are  
140 labeled with the usual atomic physics notation, i.e., with the orbital angular momentum labeled as s ( $l = 0$ ), p ( $l = 1$ ),  
141 d ( $l = 2$ ), and f ( $l = 3$ ) followed by its projection ( $m$ ) on the light propagation direction. An electric-dipole transition  
142 changes  $l$  by  $\pm 1$ , and  $m$  increases by 1 after absorbing a left-circular photon or releasing a right-circular photon.  
143 Satisfying the selection rules of both  $l$  and  $m$ , in the co-rotating case the upward pathway from the lower main peak  
144 creates a pure f3 wave and the downward pathway from the higher main peak forms a mixed wave consisting of  
145 p1 and f1. For the counter-rotating case, the populated states are the same as those in the co-rotating case. This  
146 naturally raises the interesting question what causes the CD effect on the RABBIT phase. The ratios of p1 and  
147 f1 waves in the two geometries are significantly different. Due to the Fano's propensity rule<sup>35,36</sup>, i.e., absorbing  
148 (releasing) a photon prefers to change  $l$  by +1 (-1). Thus, the sideband in the co-rotating case is dominated by the  
149 interference of f3 and p1. In contrast, in the counter-rotating case, the sideband is dominated by the interference  
150 of f3 and f1. In Figs. 3b and d, we show the interference pattern between f3 and p1 and that between f3 and f1,  
151 respectively, assuming equal partial-wave phases and amplitudes. For the co-rotating case the interference between  
152 f3 and p1 gives rise to the isotropic phase profile, and the interference between f3 and f1 for the counter-rotating  
153 case reproduces the  $\pi$ -shift structure in the RABBIT phase (as visualized by the dashed lines in panels b and d),  
154 which actually originates from the alternating sign of the three lobes of the f1 wave. Note that here the goal of this  
155 simple two-wave interference model is not a quantitative reproduction of the RABBIT phase, but to illustrate the  
156 most fundamental CD effects in the RABBIT phase.

157 After considering the amplitudes and phases of all participating partial waves, one can fully reproduce the  
158 RABBIT traces illustrated in Figs. 2g-i. The TDSE simulation naturally provides this information by expanding



159 the final wavefunction into a spherical-harmonic basis. Figures 4a-b show the calculated amplitudes and phases of  
160 the f3, p1, and f1 partial waves from the p<sub>+</sub> ground-state orbital in the co-rotating and counter-rotating geometries,  
161 respectively. In the co-rotating case, the relative amplitude ratio of these partial waves agrees well with Fano's  
162 propensity rule, i.e., the p1 wave is dominant over the f1 wave. However, in the counter-rotating case Fano's  
163 propensity rule is not entirely correct<sup>37</sup>, although the proportion of the f1 wave has obviously increased, which is  
164 enough to cause the significant variation in the RABBIT phase. In contrast, the partial-wave phases provide a unique  
165 view to the photoionization dynamics of electron vortices. The phase of the f3 wave in the co-rotating case is equal  
166 to that of the f1 wave in the counter-rotating case, and similarly the phase of the co-rotating f1 wave is equal to  
167 that of the counter-rotating f3 wave. This is because the phase of the electric dipole transition depends on *l* and the  
168 energies of initial and final states for the same azimuthal angle  $\phi$ . The phase of the p1 wave is different in the two  
169 geometries since the energies of their initial and final states are different. Therefore, the helicity of the probe light  
170 can affect not only the amplitudes of the populated partial waves, but also their phases.

171 The time- and angle-resolved RABBIT trace is a photoelectron interferogram of partial waves with specific  
172 amplitudes and phases, which provides an opportunity of completely reconstructing the time-dependent electronic  
173 superposition state by using global fittings<sup>38</sup>. Importantly, the photoelectron yield in the angular range from  
174  $\theta = 60^\circ$  to  $\theta = 120^\circ$  is dominated by ionization from the p<sub>+</sub> ground state, as illustrated in the extended-data  
175 Fig. 6d. This allows us to perform the global fitting based on the three-wave interference formula  $W_{\text{co}}(\theta, \tau) =$   
176  $|a * f_3(\theta)e^{i(\omega\tau - \phi_a)} + b * f_1(\theta)e^{-i(\omega\tau - \phi_b)} + c * p_1(\theta)e^{-i(\omega\tau - \phi_c)}|^2$  for the co-rotating case and  $W_{\text{counter}}(\theta, \tau) = |a *$   
177  $f_3(\theta)e^{-i(\omega\tau - \phi_a)} + b * f_1(\theta)e^{i(\omega\tau - \phi_b)} + c * p_1(\theta)e^{i(\omega\tau - \phi_c)}|^2$  for the counter-rotating case. A fit of this model is shown  
178 and compared with the measured interferograms in the extended-data Fig. 9, where good agreement is achieved.  
179 The six fitting parameters ( $a, b, c, \phi_a, \phi_b, \phi_c$ ) are illustrated in Figs. 4c and d for the two geometries. Our retrieved  
180 results, especially for the phases, agree well with the values extracted from the TDSE simulation within the fitting  
181 uncertainty, validating the CD effect on the transition-matrix phase of electron vortices. Because here the extracted  
182 partial-wave phases can be expressed as the sum of the phases from the two steps, i.e. the Wigner phase and the  
183 continuum-continuum phase, the phase CD between the two geometries will cancel out the Wigner phase and thus  
184 undoubtedly reveals the chirality of the continuum-continuum transition.

185 Previous experiments<sup>36,38,39</sup> have demonstrated that photoionization time delays depend on the energies and  
186 angular momenta (*l*) of both initial and final states in electronic transitions. Limited by the shortage of circularly  
187 polarized attosecond light pulses, the dependence of photoionization time delays on the magnetic quantum number  
188 (*m*) or the light helicity has not been identified prior to this work. The magnetic quantum number fundamentally

189 defines the spatial orientation and handedness of electronic wavefunctions, which plays an essential role in chiral<sup>40</sup>  
190 and topological<sup>41</sup> systems at the frontier of science. For atomic cases studied in this manuscript, the amplitude of  
191 the electron vortices does not depend on the  $\phi$  angle, and therefore the atomic electron vortices can be intuitively  
192 depicted as a doughnut shape. As for molecular systems, the wavefunction of the electron vortices has some  
193 structural/amplitude features depending on the  $\phi$  angle. The spiral phase distribution ( $e^{im\phi}$ ) of each partial wave  
194 in molecular vortices is, however, similar to the atomic case. Therefore, the ACDC effect of molecular vortices  
195 between co-rotating and counter-rotating IR probes is expected to exist. The ACDC of molecular vortices will  
196 depend on not only the  $\theta$  angle but also on the  $\phi$  angle and the orientation of molecules, providing a sensitive probe  
197 to the molecular structural and dynamical information. As a further opportunity, with the development of attosecond  
198 light source extending into the XUV and soft-X-ray regimes, inner-shell element-specific attosecond experiments  
199 have become possible. With such circularly polarized sources, the prepared electron vortices from molecular inner  
200 shells immediately after ionization will be very close to the atomic case, which offers the possibility of using ACDC  
201 to probe the effect of electron-vortex scattering in the molecular potential on attosecond time scales.

202 In summary, we have demonstrated a new technique, attosecond circular-dichroism chronoscopy. We have  
203 applied it to the complete measurement of chiral electron-photon interactions, highlighting very large CDs in both  
204 amplitude and phase. This technique in the attosecond toolbox can be applied to many other systems such as chiral  
205 molecules and topological materials. Photoelectron circular dichroism (PECD) of chiral molecules manifests itself  
206 as an amplitude asymmetry in electric-dipole transitions between forward and backward photoemission directions.  
207 The forward-backward transition-phase asymmetry has not yet been revealed, although one experiment<sup>42</sup> using  
208 femtosecond two-color fields was reported in the strong-field regime, where the results are known to depend on  
209 the intensity of the driving fields<sup>43</sup>. ACDC will enable such attosecond experiments on chiral molecules in the  
210 perturbative regime, where the results do not depend on intensity and thus reflect the inherent chiral properties  
211 of the native systems. Looking further ahead, the full exploitation of electron-ion coincidence measurements or  
212 the combination with laser-induced molecular-alignment techniques, will additionally give access to the phase  
213 asymmetry of PECD in the molecular frame, defining fully differential attosecond time-resolved chiral chronoscopy.

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## 219 Author Contributions Statement

220 M.H. performed the experiments with the support of J.J. and T. B.. M.H. and H.J.W. analyzed and interpreted the  
221 data. Simulations were implemented by M.H.. H.J.W. conceived the study and supervised its realization. All authors  
222 discussed the results and wrote the paper.

## 223 Competing Interests Statement

224 All co-authors have seen and agree with the contents of the manuscript and there is no financial interest to report.

## 225 Figure Legends/Captions

226 **Figure1: Experimental results of the CD effects on continuum-continuum transitions of the electron vortex.** **a**,  
227 Schematic illustration of the attosecond circular-dichroism chronoscopy experiment. The electron vortex (donut  
228 shape with spiral phase distribution) created by photoionization of a left circularly polarized XUV field (purple  
229 arrow) is probed by a co-rotating (red arrow) or counter-rotating (blue arrow) IR field. **b**, Measured angle-resolved  
230 photoelectron energy spectrum in the XUV-only case. **c, d**, Measured delay-integrated angle-resolved photoelectron  
231 energy spectrum after adding a co-rotating (c) and counter-rotating (d) IR field, respectively. In b-d, the photoelectron  
232 emission angle in the co-polarization plane, i.e.,  $\phi = \arctan(p_y/p_x)$ , was integrated from 0 to  $2\pi$ . **e**, Measured  
233 photoelectron energy spectra and the corresponding CD spectrum in the polarization plane, i.e.,  $\theta = \arccos(p_z/p_{\text{total}})$   
234  $= 90^\circ$ . **f, g**, Measured delay- and angle-resolved photoelectron distributions of SB12 in the co-rotating (f) and  
235 counter-rotating (g) cases. **h**, Extracted angle-resolved RABBIT phases from f and g using Fourier transformation.  
236 The uncertainty (shade area) is estimated by the B/A approach<sup>44</sup>. These two RABBIT-phase curves are also plotted  
237 in f and g with dashed lines.

238 **Figure2: TDSE simulations.** **a, b**, TDSE simulations of the delay-integrated angle-resolved photoelectron  
239 energy spectra in the co-rotating (a) and counter-rotating (b) geometries. **c**, Photoelectron energy spectra and the  
240 corresponding CD spectrum in the light polarization plane. **d, e**, Delay- and angle-resolved photoelectron spectra of  
241 sideband 12 in the co-rotating (d) and counter-rotating (e) geometries. **f**, Extracted angle-resolved RABBIT phases  
242 from d and e. Note that in a-f the results are averaged over the photoelectron momentum distributions from the  
243 degenerate  $p_+$ ,  $p_-$  and  $p_0$  orbitals. **g-i**, The corresponding results from the  $p_+$  orbital alone.

244 **Figure3: Interference mechanism in co-rotating and counter-rotating geometries based on the  $p_+$  ground**  
245 **state.** **a, c**, Energy-level diagrams for the co-rotating probe (a) and the counter-rotating probe (c). The dominant  
246 contributions according to Fano's propensity rule are labeled with bold letters. **b, d**, Simplified two-wave interference

247 pattern between f3 and p1 for the co-rotating case (b), and that between f3 and f1 for the counter-rotating case (d).  
248 In b and d, the dashed curves depict the extracted RABBIT phases.

249 **Figure4: Amplitude and phase of the relevant partial waves at sideband 12.** **a, b**, TDSE Results from the p<sub>+</sub>  
250 ground-state orbital for the co-rotating and counter-rotating geometries, respectively. **c, d**, Global-fitting results of  
251 the experimental data for the two polarization configurations. Note that the amplitudes are normalized to the sum  
252 in each case. The error bars and the shaded areas in c and d represent the 95% confidence intervals for the fitting  
253 parameters obtained by nonlinear regression.

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## 339 **Methods**

340 **Experimental details.** Our experimental setup is illustrated in the extended-data Fig. 5. Near-infrared laser pulses  
341 (2 mJ) were delivered from a regenerative Ti:sapphire laser amplifier at a central wavelength of 800 nm with the  
342 repetition rate of 5 kHz. A pulse duration of 25 fs for the full width of half maximum in intensity was measured  
343 by a home-built FROG apparatus. This laser beam was split with a 70:30 beam splitter, and the more intense part  
344 was sent through our beam-in-beam module and then focused by a silver mirror ( $f = 35$  cm) into a 4 mm long,  
345 xenon-filled gas cell to generate a circularly polarized extreme-ultraviolet attosecond pulse train via high-harmonic  
346 generation. Our beam-in-beam module consists of a specially designed half waveplate and a common quarter  
347 waveplate. The half waveplate is composed of two half disks and the relative angle between the fast axes of the two  
348 parts is  $45^\circ$ . For example, in our case the fast axes are oriented at  $\pm 22.5^\circ$  with respect to the horizontal boundary,  
349 respectively. After passing through this half waveplate, the polarization directions of the upper part and the bottom  
350 part of the beam are orthogonal to each other. The two parts of the beam are then converted to be circularly polarized  
351 but with opposite helicities by transmission through the quarter waveplate. The left-circularly polarized XUV  
352 beam in the two produced beams was picked up using a perforated mirror and focused into the main chamber  
353 of a COLTRIMS by a nickel-coated toroidal mirror ( $f = 50$  cm). The XUV spectrum was characterized with a  
354 home-built XUV spectrometer consisting of an aberration-corrected flat-field grating (Shimadzu 1200 lines/mm)  
355 and a micro-channel-plate (MCP) detector coupled to a phosphor screen. We completely characterized the Stokes  
356 parameters and the temporal structure of our XUV pulses. In the attosecond pulse train, the duration of each of the  
357 composite attopulses was measured as  $\sim 940$  as for the amplitude FWHM, corresponding to 480 as for the intensity  
358 FWHM. The ellipticities of the harmonics are 0.98, 0.94 and 0.87 for H11, H13 and H15, respectively. The IR beam  
359 with 30% energy was used as the dressing field in RABBIT experiments. The dressing IR field was adjusted to

360 left- or right-circular polarization by a zero-order quarter waveplate and its intensity was controlled at a very low  
 361 level (about  $10^{12}$  W/cm<sup>2</sup>) by an iris. The dressing IR beam was focused by a perforated lens ( $f = 50$  cm) and then  
 362 recombined with the XUV beam by a perforated mirror. In the arm of the dressing field, there were two delay stages,  
 363 i.e., a high-precision direct-current motor (PI, resolution 100 nm) and a piezoelectric motor (PI, resolution 0.1 nm),  
 364 adjusting the interpulse delays on femtosecond and attosecond time scales, respectively. A HeNe continuous-wave  
 365 laser beam was sent through the beam splitter and traced the IR path in the two arms of the interferometer. A fast  
 366 CCD camera behind the recombination mirror was used to lock the phase delay between the two arms through a  
 367 PID feedback. When scanning the XUV-IR phase delay in the measurements, the piezo delay stage was actively  
 368 stabilized at the step size of 156 as with the time jitter of less than 30 as. For the COLTRIMS setup, the supersonic  
 369 gas jet of argon atoms (backing pressure of 1 bar) was delivered along the  $x$  direction by a small nozzle with an  
 370 opening hole diameter of  $30 \mu\text{m}$  and passed through two conical skimmers (Beam Dynamics) located 10 mm and 30  
 371 mm downstream with a diameter of 0.2 mm and 1 mm, respectively. For the COLTRIMS spectrometer, static electric  
 372 ( $\sim 2.21$  V/cm) and magnetic ( $\sim 5.92$  G) fields were applied along the  $y$  axis to collect the charged fragments in  
 373 coincidence. Only the single ionization (one electron is coincident with one  $\text{Ar}^+$ ) events are presented in this work.

374 **TDSE simulation.** We performed the TDSE simulations based on an open-source TDSE solver, Qprop 2.0<sup>34</sup>,  
 375 where the details of the algorithm and the source code are available. In the simulation, we used the model potential  
 376  $V_{\text{eff}} = -[Z + (Z_{\text{full}} - Z)\exp(-r_s \cdot r)]/r$  within the single-electron-approximation, where  $Z = 1$  and  $Z_{\text{full}} = 18$  are  
 377 the asymptotic ion charges as  $r \rightarrow \infty$  and  $r \rightarrow 0$ , respectively. The screening length  $r_s = 0.2149$  is used to match  
 378 the ionization potential  $I_p = 15.6$  eV of argon. The initial magnetic quantum number  $m$  was tuned to be 1, 0 and  
 379 -1 without changing the ionization potential, respectively. The final photoelectron momentum distribution was  
 380 averaged non-coherently over these three degenerate orbitals. The vector potential of the XUV field is  $A_{\text{XUV}}(t) =$   
 381  $-A_{\text{XUV}}^0 \sum_{i=11,13,15,17} \sin^2(\omega t/2n_c) * [\sin(i\omega t)\vec{x} + \cos(i\omega t)\vec{y}]$  and that of the IR field is  $A_{\text{IR}}(t) = -A_{\text{IR}}^0 \sin^2(\omega t/2n_c) *$   
 382  $[\sin(\omega(t + \tau))\vec{x} + \cos(\omega(t + \tau))\vec{y}]$ , where the amplitude  $A_{\text{XUV}}^0 = 0.00534$  a.u.,  $A_{\text{IR}}^0 = 0.0033$  a.u., the pulse duration  
 383 amounts to  $n_c = 6$  optical cycles, and the XUV-IR delay  $\tau$  was uniformly sampled by 24 points in one IR cycle.  
 384 The discretization box used for the simulations had a radial box size of 150 a.u. with the grid size of 0.2 a.u.. The  
 385 maximum angular momentum included is  $l_{\text{max}} = 15$ , which is big enough to cover all ionized electronic partial waves.  
 386 The time step was  $\Delta t = 0.04$  a.u.. To avoid unwanted reflections from the boundaries, a complex boundary absorber  
 387 was placed starting at 100 a.u. before the end of the simulation. The convergence of the numerical calculations  
 388 has been checked with respect to all discretization parameters. Qprop has two different expansion modes for the  
 389 finally obtained wavefunction depending on which kinds of physical variables are being extracted. When showing



390 the calculated angular distribution of photoelectrons, the first expansion mode was used and the Jacobian matrix  
 391  $(\sin\theta)$  was taken into account. The momentum box was set from 0.1 a.u. to 1.1 a.u. with 100 bins, and there are 91  
 392 uniform bins for  $\phi = \arctan(p_y/p_x)$  in the  $2\pi$  range and 19 uniform bins for  $\theta = \arccos(p_z/p_{\text{total}})$  in the  $\pi$  range.  
 393 When displaying the calculated amplitudes and phases of all populated partial waves, the second expansion mode  
 394 was used.

395 **Analytical perspective of the continuum-continuum transition matrix element.** Here we consider the helium case  
 396 which corresponds to the previous study<sup>33</sup>. After absorbing a left CP XUV photon, the electronic state at the main  
 397 peak is the  $p_{+1}$  state. Then absorbing a co-rotating IR photon, the electronic state at the sideband is the  $d_{+2}$  state,  
 398 and the corresponding continuum-continuum transition probability can be expressed as the product of radial and  
 399 angular integrals,  $Y_{\text{co}} = |\langle \Psi_{\varepsilon d}(r) | \hat{r} | \Psi_{\varepsilon p}(r) \rangle|^2 * |\langle Y_{22}(\theta, \phi) | Y_{11}(\theta, \phi) | Y_{11}(\theta, \phi) \rangle|^2 = |\langle \Psi_{\varepsilon d}(r) | \hat{r} | \Psi_{\varepsilon p}(r) \rangle|^2 * \frac{3}{10\pi}$ ,  
 400 where the angular integral is calculated using the Gaunt coefficients. In the counter-rotating IR probe, the  
 401 populated states are  $d_0$  and  $s$  states, and the transition probability is  $Y_{\text{counter}} = |\langle \Psi_{\varepsilon d}(r) | \hat{r} | \Psi_{\varepsilon p}(r) \rangle|^2 * \frac{1}{20\pi} + |\langle \Psi_{\varepsilon s}(r) | \hat{r} | \Psi_{\varepsilon p}(r) \rangle|^2 * \frac{1}{4\pi}$ .  $Y_{\text{co}} > Y_{\text{counter}}$  gives rise to the condition that  $|\langle \Psi_{\varepsilon d}(r) | \hat{r} | \Psi_{\varepsilon p}(r) \rangle|^2$  is larger than  
 402  $|\langle \Psi_{\varepsilon s}(r) | \hat{r} | \Psi_{\varepsilon p}(r) \rangle|^2$ , which is exactly the Fano's propensity rule in the continuum-continuum transition (see  
 403 Fig. 4 in a previous theoretical study<sup>45</sup>) when the photon energy is away from Cooper minimum or autoionization  
 404 states. Therefore, the total sideband yield in the co-rotating geometry is larger than that in the counter-rotating  
 405 geometry. In the extended data Fig. 9, we show the TDSE simulations on helium atoms and similar amplitude and  
 406 phase CDs are validated.

## 408 Data availability

409 Source data are available for this paper. All other data that support the plots within this paper and other findings of  
 410 this study are available from the corresponding author (M.H.) upon reasonable request.