

# H<sub>2</sub> lines from the first generation star formation process

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*H<sub>2</sub> lines from  
the first-generation star  
formation process*

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# Abstract

Molecular hydrogen line photons emitted owing to formation events of first-generation stars and their detectability by future observational facilities are explored. The H<sub>2</sub> luminosity evolution from the onset of prestellar collapse to the formation of a  $\sim 100 M_{\text{sun}}$  protostar is followed by a simplified model for the dynamical evolution. In particular, the calculation is extended not only the early phase of the runaway collapse but also to the later phase of accretion, whose observational feature has not been studied before. Contrary to the runaway collapse phase, where the pure-rotational lines are always dominant, during the accretion phase prominent emission is owing to rovibrational lines. Also, the maximum luminosity is attained in the accretion phase for strong emission lines. The peak intensity of the strongest rovibrational line reaches  $\sim 10^{-27}$  (W/m<sup>2</sup>), corresponding to the flux density of  $10^{-5}$  ( $\mu$  Jy), for a source at the typical redshift of the next-generation infrared satellite, SPICA, *Space Infrared Telescope for Cosmology and Astrophysics*, is ideal for observing the redshifted rovibrational line emission, to exceed the detection threshold, about  $10^6$  such forming stars must reach the maximum luminosity simultaneously in a pregalactic cloud. Unfortunately, this situation is excluded by the current theoretical understanding of early structure formation.

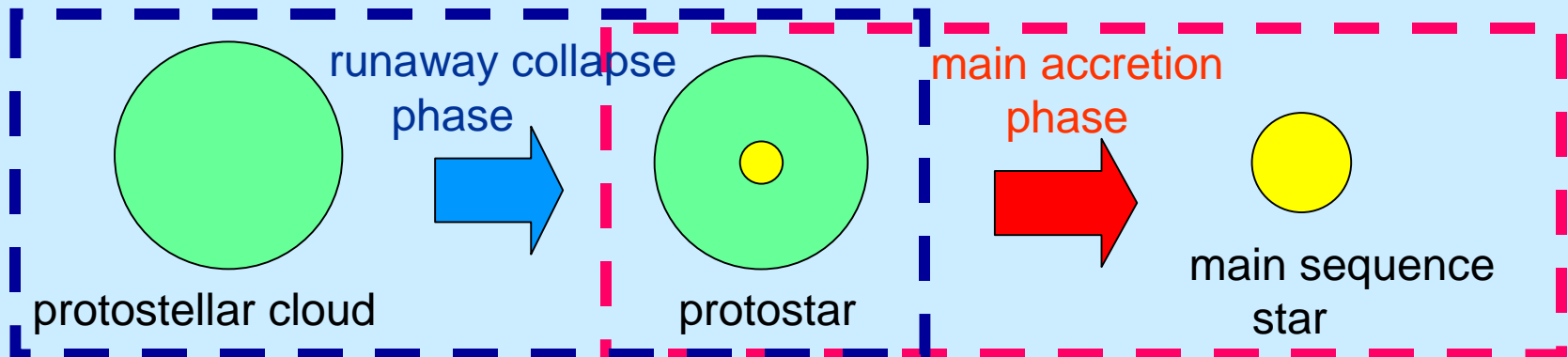
# Purpose

We estimate **the luminosities of  $H_2$  lines**, which can be characteristics of the first star formation process, and evaluate **the detectability of  $H_2$  lines**.

The luminosities of  $H_2$  lines for **the runaway collapse phase**  
→ Ripamonti et al (2002) and Kamaya & Silk (2002)

However the luminosities of  $H_2$  lines  
for **the main accretion phase** haven't been estimated.

→ we calculate them for both phase .

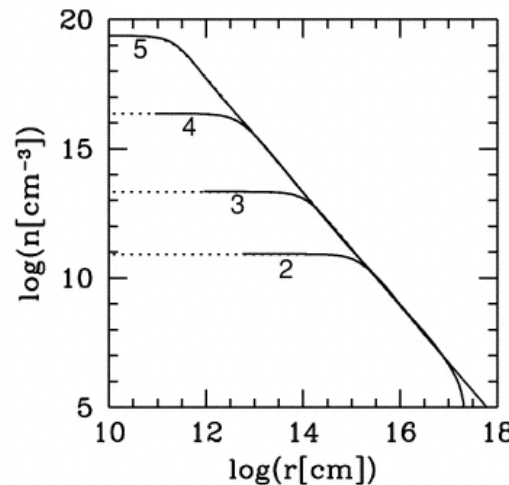
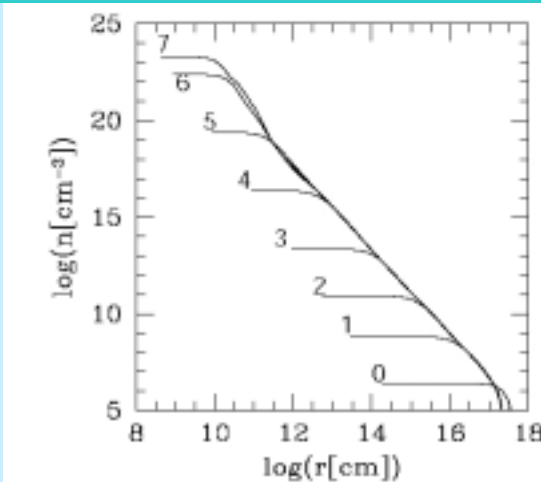


# Model

The thermal and chemical evolution of gravitationally collapsing protostellar clouds is investigated by hydrodynamical calculations for spherically symmetric clouds.

(Omukai&Nishi 1998)

## The evolutionary sequences



## The time interval

- 0 → 1 ~  $5.7 \times 10^5$  yr
- 1 → 2 ~  $8.7 \times 10^3$  yr
- 2 → 3 ~  $2.8 \times 10^2$  yr
- 3 → 4 ~ 12 yr
- 4 → 5 ~ 0.32 yr
- 5 → 6 ~  $2.4 \times 10^{-2}$  yr
- 6 → 7 ~  $4.1 \times 10^{-2}$  yr

The Larson-Penston-type similarity solution,  $\gamma = 1.09$  (dotted line), reproduces Omukai&Nishi's result (solid line) well.


It is a good approximation to the actual collapse dynamics.

**center** ---- flat density distribution, runaway collapse  
**envelope** ---- leaving the outer part practically unchanged

We focus on the central region and calculate the time evolution (e.g., Omukai 2000).

# 1. Dynamics

## · *The runaway collapse phase*

The central evolution  the free-fall relation modified by pressure gradient

$$\frac{d\rho}{dt} = \frac{\rho}{\beta t_{\text{ff}}} \quad , \quad t_{\text{ff}} = \sqrt{\frac{3\pi}{32 G \rho}} \quad \begin{array}{l} \rho : \text{the central density} \\ t_{\text{ff}} : \text{free-fall time} \end{array}$$

the collapse time scale ;  $\beta t_{\text{ff}}$       the flat core size ;  $\alpha \lambda_J$

The modification due to the finite pressure gradient force is represented

by the correction factor  $\alpha, \beta$ .

For the Larson-Penston-type similarity solution for  $\gamma = 1.09$ ,

$$\delta = \left| \frac{\text{pressure}}{\text{gravity}} \right| \cong 0.78 \quad , \quad \alpha = \sqrt{1 + \delta} \quad , \quad \beta = \frac{1}{\sqrt{1 - \delta}} \quad , \quad \alpha = 1.33 \quad , \quad \beta = 2.13$$

## · *The main accretion phase*

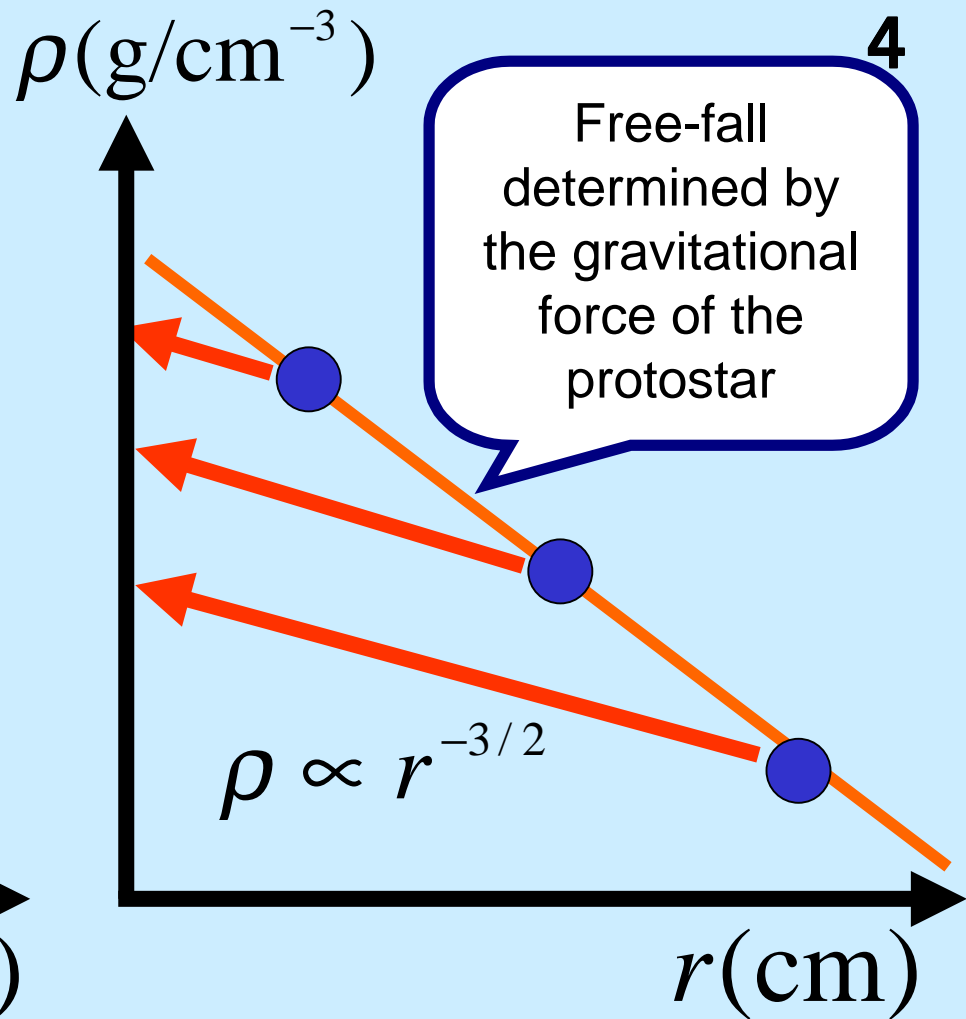
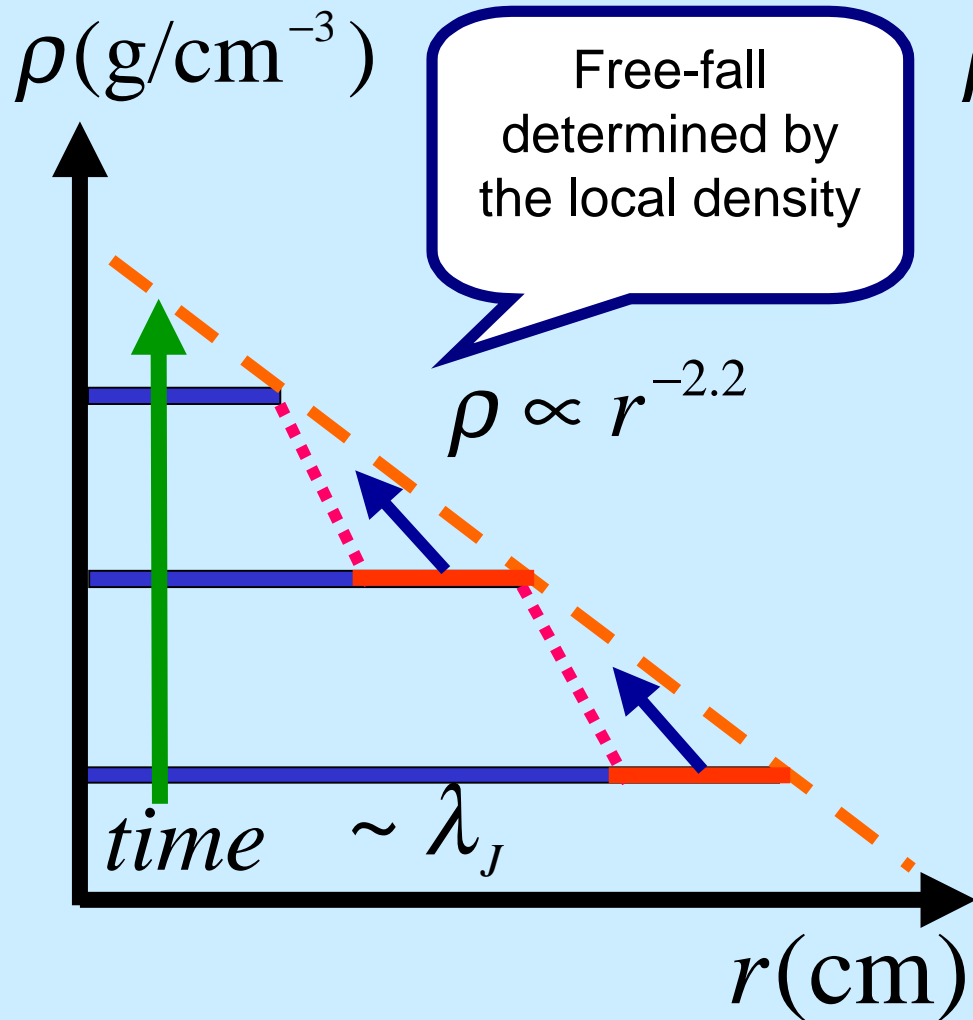
approximation, each mass shell  free-fall

$$\frac{dv_r}{dt} = -\frac{GM(< r)}{r^2} \quad , \quad \frac{dr}{dt} = -v_r \quad , \quad \rho \propto r^{-3/2}$$

$\rho$  : the density of  
free-falling mass shell

$v_r$  : the velocity of  
free-falling mass shell

$r$  : the distance from mass shell  
to the center



## 2. Energy equation

$$\frac{de}{dt} = -p \frac{d}{dt} \left( \frac{1}{\rho} \right) - L^{(net)}$$

$$e = \frac{1}{\gamma - 1} \frac{kT}{\mu m_H}, \quad p = \frac{\rho kT}{\mu m_H}$$

$e$  : the energy per unit mass ,  $p$ : the pressure ,  $T$ : the temperature ,

$\gamma$  : the adiabatic exponent ,  $\mu$  : the mean molecular weight ,

$m_H$ : the mass of the hydrogen nucleus

## 3. Cooling/Heating processes

$$L^{(net)} = L_{rad} + L_{chem} , \quad L_{rad} = L_{line} (+L_{cont})$$

$L_{rad}$  : the radiative cooling rate,  $L_{chem}$  : the chemical cooling rate or heating rate,

$L_{line}$  : the cooling rate of line emission,  $L_{cont}$  : the cooling rate of continuum emission

The continuum cooling rate  $L_{cont}$  is treated with the radiation field from the central protostar which is assumed to be the black body of 6000 K.



# • line cooling

$$L_{\text{H}_2} = \frac{1}{\rho} \sum_{i \rightarrow j} n(\text{H}_2, i) A_{ij} \epsilon_{ij} h \nu_{ij}$$

$$n(\text{H}_2, i) \sum_{j \neq i}^n R_{ij} = \sum_{j \neq i}^n n(\text{H}_2, j) R_{ji}$$

$$R_{ij} = \begin{cases} A_{ij} \epsilon_{ij} + C_{ij} & (i \geq j) \\ C_{ij} & (i \leq j) \end{cases}$$

$$\epsilon_{ij} = \frac{1 - e^{-\tau_{ij}}}{\tau_{ij}}$$

$$\tau_{ij} = \frac{A_{ij} c^3}{8\pi \nu_{ij}^3} \left[ n(x, j) \frac{g_i}{g_j} - n(x, i) \right] l_{\text{sh}} / (2\Delta v_D)$$

$$l_{\text{sh}} = \min(\Delta S_{\text{th}}, \alpha \lambda_J / 2), \quad \Delta v_D = \sqrt{2kT / (\mu m_{\text{H}})}$$

The runaway collapse phase ;

$$\Delta S_{\text{th}} = 2\Delta v_D / (dv/dr) = 6\Delta v_D \beta t_{\text{ff}}$$

The main accretion phase ;

$$\Delta S_{\text{th}} = 2\Delta v_D / (dv/dr) = 2\Delta v_D / \left( \frac{GM}{vr^2} \right) = 2\sqrt{2}\Delta v_D \frac{r^{3/2}}{\sqrt{GM}}$$

$n(\text{H}_2, i)$  --- the population density of  $\text{H}_2$  in level  $i$

$A_{ij}$  --- the spontaneous transition probability

$\epsilon_{ij}$  --- the escape probability

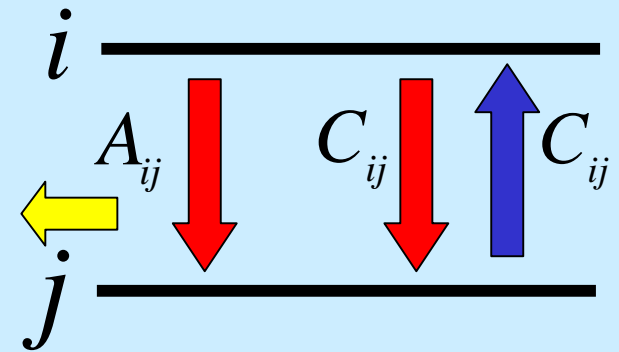
$h\nu_{ij}$  --- the energy difference between levels  $i$  and  $j$

$C_{ij}$  --- the collisional transition rate from level  $i$  to level  $j$

$\Delta v_D$  --- the velocity dispersion

$l_{\text{sh}}$  --- the shielding length

$\tau_{ij}$  --- the optical depth averaged over the line



• *continuum cooling/heating*

The main continuum processes as the radiative effect of the protostar



bound-free absorption of  $\text{H}^-$ ,  
free-free absorption of  $\text{H}^-$ ,  
 $\text{H}_2$  collision induced absorption

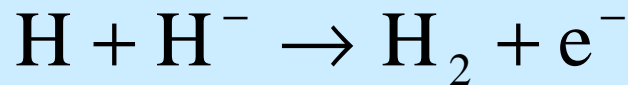
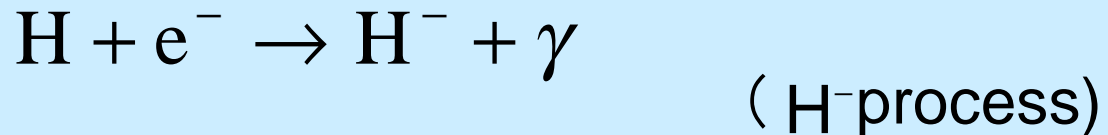
$$\Lambda_{cont}(\nu) = 4\pi[\eta_a(\nu) - \kappa_a(\nu)J(\nu)]$$

$\eta_a(\nu)$ : the thermal part of emission coefficient

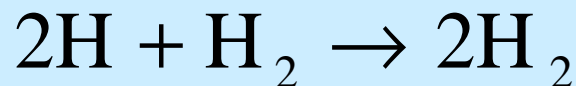
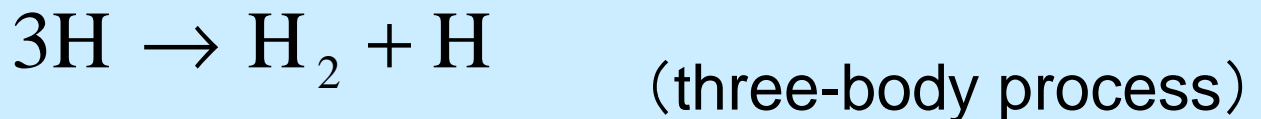
$\kappa_a(\nu)$ : the absorption coefficient,  $J(\nu)$ : the intensity of the central protostar

#### 4. Chemical reactions ( $\text{H}_2$ formation processes)

$$n_{\text{H}} (\sim 10^8 \text{ cm}^{-3})$$



$$n_{\text{H}} (10^8 \text{ cm}^{-3} \sim 10^{14} \text{ cm}^{-3})$$



# Initial Conditions

The contraction and fragmentation of primordial, metal-free gas clouds is investigated by several authors . (e.g., Uehara et al. 1996; Abel et al. 2002; Bromm et al. 2002; Nakamura & Umemura 2002)

We adopt the typical values for the star-forming cores from Bromm et al.(2002).

## The physical condition of fragments (protopstellar clouds)

$$M_J \sim 10^3 M_{\text{sun}} \quad M_J : \text{Jeans mass}$$

$$n_{\text{H}} = 10^4 (\text{cm}^{-3}), T = 500(\text{K}), y(\text{H}_2) = 10^{-3}, y(\text{e}^-) = 10^{-8}$$

$y(\text{H}_i) = n(\text{H}_i) / n(\text{H})$  : the concentration of the  $i$ -th species

$n(\text{H})$  : the number density of the hydrogen nucleus

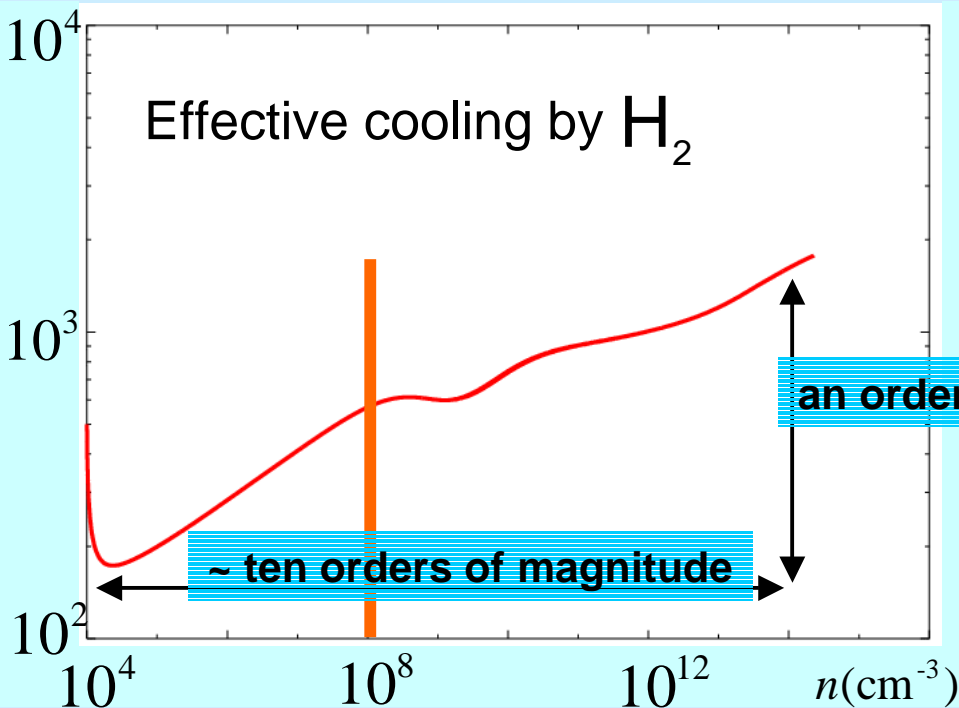
# Results

★ *Notice!*

temperature, abundance of  $H_2$ ,  
luminosities of the  $H_2$  lines

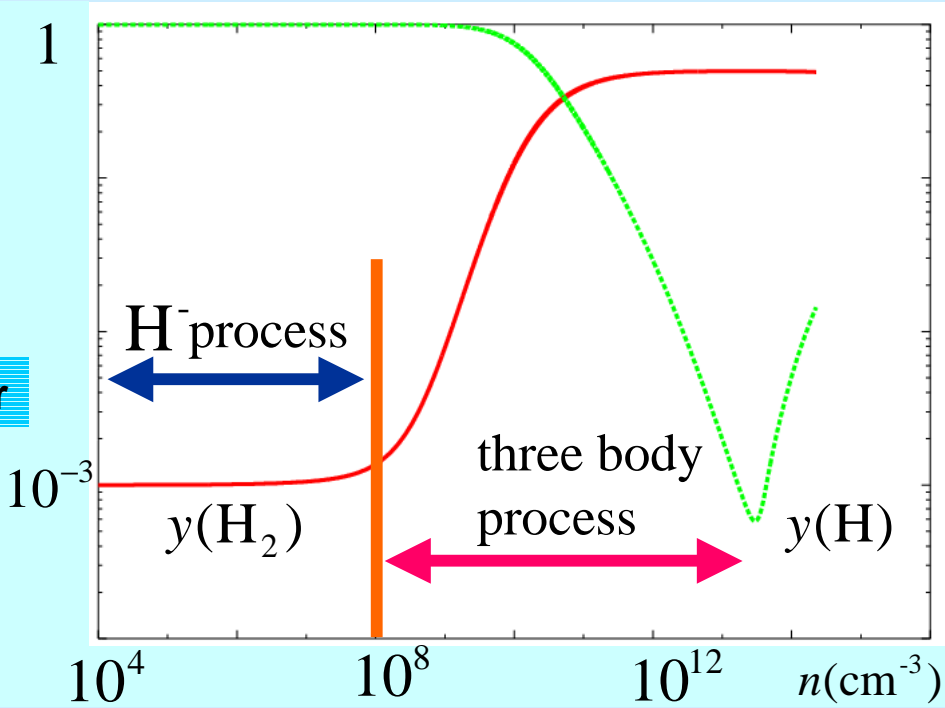
## The runaway collapse phase

$T(K)$  The time evolution of the central temperature



time

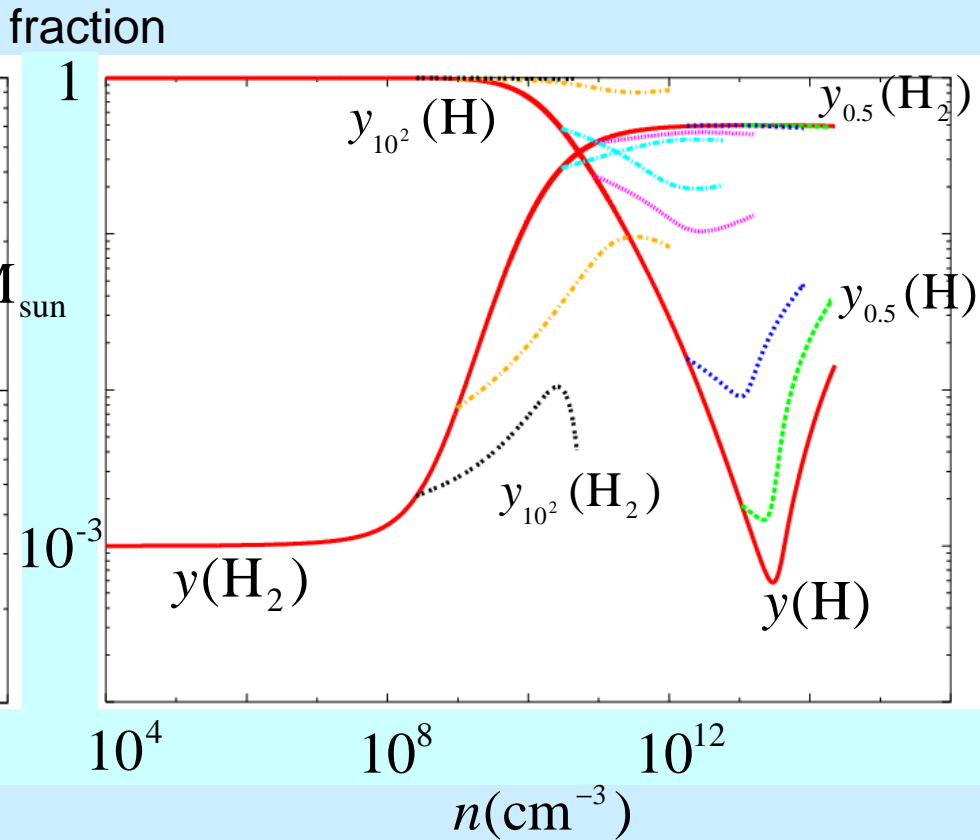
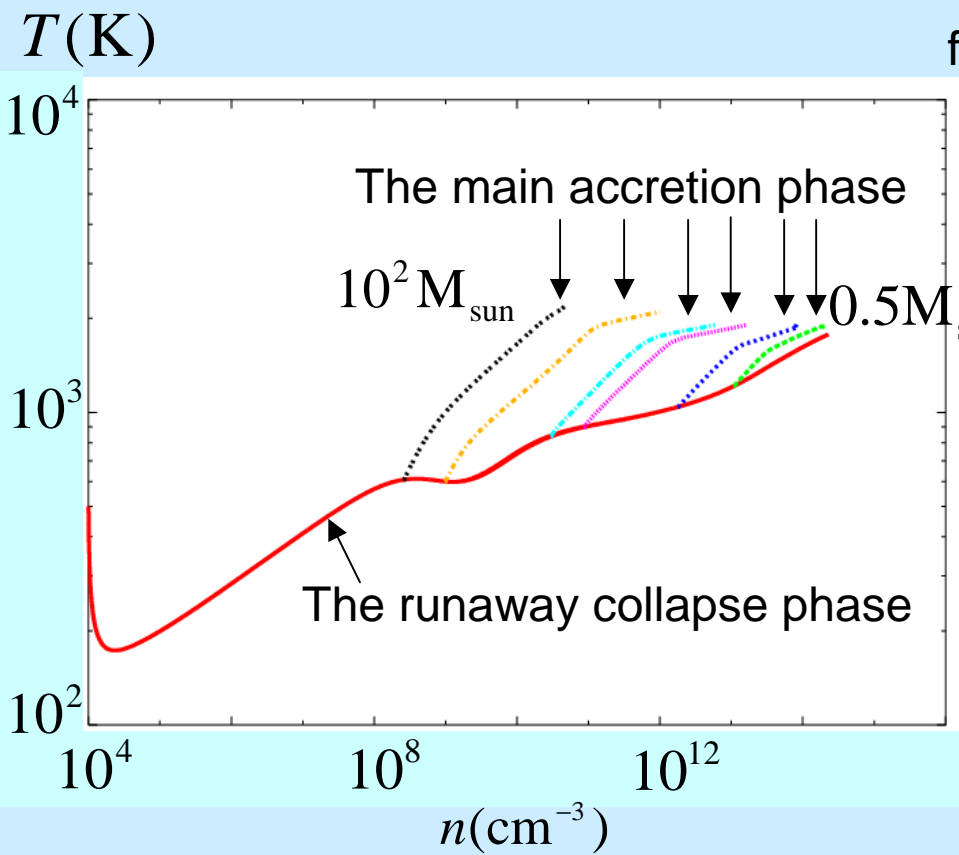
fraction The time evolution of the central abundance of  $H, H_2$



time

# Comparison between runaway collapse phase and main accretion phase

For the accretion phase, the evolutionary trajectories of the mass shells of  $M / M_{\text{sun}}$  ( $M$  : protostellar mass) = 0.5, 1, 5, 10, 50, 100 are shown.



time →

time →

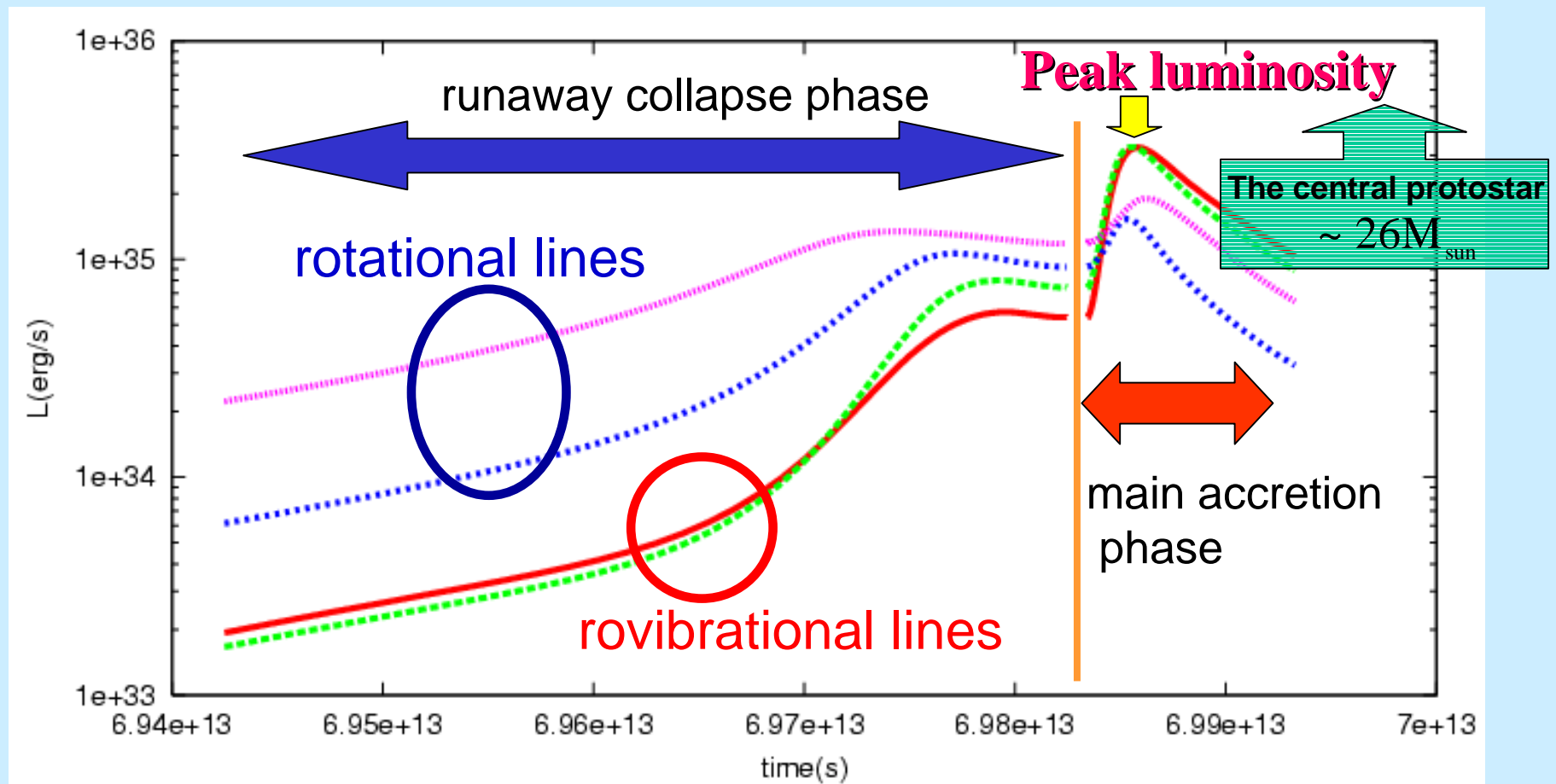
# The time evolution of the $H_2$ line luminosities

**Pick up** : four of the strongest  $H_2$  lines

**red**: (1,1)→(0,1), **green**: (1,1)→(0,3), **blue**: (0,6)→(0,4), **purple**: (0,5)→(0,3)

rest frame : 2.34  $\mu m$  , 2.69  $\mu m$  , 8.27  $\mu m$  , 10.03  $\mu m$

**before** (vibrational level, rotational level) → **after** (vibrational level, rotational level)



# Detectability

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**For mid-infrared region** ( $\lambda \sim 40\mu\text{m}$ ), **SPICA**(ISAS), a large(3.5m),cooled(4.5K) telescope, is **the best** . (better than JWST and ALMA)

The line detection limit of **SPICA** is about  $10^{-20}$  ( $\text{W}/\text{m}^2$ ) in  $\lambda \sim 40\mu\text{m}$ . In this region, the high background of the zodiacal light limits the sensitivity of SPICA to  $10^{-(21-22)}$  ( $\text{W}/\text{m}^2$ ) (private communication H.Matsuhara).

(1,1)  $\rightarrow$  (0,1), rest frame:  $\lambda = 2.34(\mu\text{m})$   
redshifted( $1+z=20$ ):  $\lambda = 46.8(\mu\text{m})$

$$F_{\text{peak}} = \frac{L_{\text{peak}}}{4\pi D_{z=19}^2} \sim 10^{-27} (\text{W} / \text{m}^2)$$

$D_{z=19}$ : The luminosity distance to  $z=19$   
 $L_{\text{peak}}$ : The peak luminosity

If there are more than  $10^{5-6}$  sources with their luminosity near the peak value, **SPICA** is able to observe a cluster of forming first-generation stars.




The total cloud mass reaches Galactic scale.

The metallicity in the pregalactic clouds must be lower than  $\sim 10^{-4} Z_{\text{sun}}$  (Omukai 2000).

Formation of Galactic scale with such low metallicity is clearly excluded in the context of standard cosmology (e.g., Scannapieco, Schneider, & Ferrara 2003)

# Summary

- We estimate the  $H_2$  line luminosities from the first-generation star formation process.
- the luminosities of both **rovibrational lines** and **rotational lines** become maximum value at **the main accretion phase**.
- For the runaway collapse phase, the strongest lines are **rotational lines**. But for **the main accretion phase**, some **rovibrational lines** overwhelm them.
- For the peak, **rovibrational lines** are stronger than **rotational lines**.

**rotational lines** ----- low density region such as envelope of the protostellar clouds  
**rovibrational lines** ----- high density region such as final stage of star formation process  
**rovibrational lines**  **the evidence** of the first-generation star formation

For observation of the first-generation star **rovibrational lines are important**.

- Unfortunately, detecting  $H_2$  line emission from forming first star by SPICA is highly improbable.