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## Complete characterization of sub-Coulomb-barrier

### <sup>2</sup> tunneling with phase-of-phase attoclock

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#### 14 ABSTRACT

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Laser-induced electron tunneling, triggering a broad range of ultrafast phenomena such as the generation of attosecond light pulses, photoelectron diffraction and holography, has laid the foundation of strong-field physics and attosecond science. Using the attoclock constructed by single-color elliptically polarized laser fields, previous experiments have measured the tunneling rates, exit positions, exit velocities and delay times for some specific electron trajectories, which are mostly born at the field peak instant where the laser electric field and the formed potential barrier are stationary in terms of the derivative versus time. From the view of the wave-particle dualism, the electron phase under a classically forbidden, tunneling barrier has not been measured, which is at the heart of quantum tunneling physics. Here we present a robust measurement of tunneling dynamics including the electron sub-barrier phase and amplitude. We combine attoclock technique with two-color phase-of-the-phase spectroscopy to accurately calibrate the angular streaking relation and to probe the non-stationary tunneling dynamics by manipulating a rapidly changing potential barrier. This phase-of-phase attoclock (POP attoclock) directly links the measured phase of the two-color relative phase with the ionization instant for the photoelectron with any final momentum on the "detector", which allows us to reconstruct the imaginary tunneling time and the accumulated phase under the barrier. The POP attoclock provides a general time-resolved approach to access the underlying quantum dynamics in intense-light-matter interactions.

The tunneling of a micro-particle through a barrier is one of the most fundamental and ubiquitous quantum 16 processes. In strong-field ionization the oscillating electric field of laser pulses creates a time-dependent potential 17 barrier in atoms or molecules allowing the bound electron to tunnel. At the instant of the field peak the potential 18 barrier is the thinnest and stationary as the derivative versus time is zero. After the peak instant, the potential barrier 19 changes quickly on the attosecond timescale, still triggering a series of tunneling bursts or electrons with different 20 probabilities at different positions. This sub-cycle electron dynamics greatly enriches strong-field phenomena<sup>1</sup>, 21 ranging from strong-field ionization to high-order harmonic emission. Previous measurements mainly focus on the 22 most probable tunneling burst which is born at the instant of the field peak, such as the efforts on the tunneling 23 time delay $^{2-11}$ , exit velocities $^{12-14}$  and exit positions $^{15-17}$ . In contrast, the tunneling dynamics under a classically 24 forbidden, non-stationary barrier is less explored, especially for the electron sub-barrier phase, which is essential to 25 fully understand and characterize this fundamental quantum mechanical process. 26

The sub-cycle tunneling bursts could be mapped to different emitting angles within elliptically or circularly 27 polarized light fields, which is the principle of the attoclock<sup>2,3</sup>. There, the mapping relation between the final 28 photoelectron momentum p and its ionization instant t relies on an important, but unproved assumption that the 29 angle-time mapping is angularly uniform. For the photoelectron with the maximum yield in the final momentum 30 space, it is clear that it originates from the tunneling burst born at the instant of the electric-field peak. However, as 31 for the photoelectron with a general momentum (e.g., see the red box in Figure 1a), actually one cannot determine 32 its ionization instant without the assumption of the uniform mapping. Indeed, as we shown in this work, this 33 assumption is not valid (i.e., the rotation angle of the electric field vector  $\beta_{\omega}$  is not identical to that of the electron 34 momentum vector  $\alpha_p$  in Figure 1a). To realize the time-resolved ability in the full momentum space, determining 35 the ionization instant of each non-stationary tunneling burst and probing its sub-Coulomb barrier dynamics become 36 the key challenges in ultrafast science. 37

Recently, the phase-of-phase photoelectron spectroscopy was introduced to extract the scattering structural information of atoms, molecules and nanoparticles<sup>18–23</sup>, in which the momentum-resolved electron yield is Fourier transformed with respect to the relative phase between two-color laser fields to obtain the phase of the yield oscillation, which is the so-called phase of the phase. The phase-of-phase spectrum provides rich dynamical information than the static photoelectron spectra measured in the one-color field. However, the physical meaning of the obtained phase of the phase is not straightforward and thus the application of this elegant time-resolved photoelectron spectroscopy is limited.

<sup>45</sup> Here we introduce phase-of-phase attoclock (POP attoclock) spectroscopy, i.e., combining the attoclock and



Figure 1: Phase-of-phase attoclock photoelectron spectroscopy. a, Measured photoelectron momentum distribution in a common attoclock configuration, in which a strong elliptically polarized 800-nm fundamental wave (FW, indicated by a red ellipse in the inset) is used to trigger a series of tunneling bursts following the rotating electric-field vector. The red dashed arrow and the red solid arrow identify the static tunneling at the field crest and the non-stationary tunneling in the falling edge, respectively. At the two ionization instants, the change tendency of the potential barrier is different, which is indicated by the crooked orange arrows near the barrier. Different sub-barrier dynamics gives rise to the different phase distribution on the emitting electron wave-packet (indicated by the color). **b**, Calibration of the relative phase in the POP attoclock configuration, in which a weak co-rotating circularly polarized second harmonic (SH) field is added into the common attoclock. The left panel shows the defined zero point for the relative phase, where the two fields both point to the vertical upward direction at the ionization instant of t = 0 so that the barrier will be bent to the maximum extent and its corresponding electron lobe in the final momentum plane (i.e., the left lobe) will reach the yield maximum. The right panel shows measured photoelectron energy spectrum for the left electron lobe as a function of the relative phase between two fields, from which we can accurately calibrate the relative phase between two fields. Here the emitting angle  $\theta = \operatorname{atan}(p_z/p_x)$ was integrated from 70° to 250°. c, Measured photoelectron momentum distributions at the relative phases of 0,  $\pi/6$ ,  $\pi/3$ . **d**, Measured phase-resolved electron yield (blue dots) for a given photoelectron momentum [ $(p_x, p_z)$  = (-0.2, 0.74) a.u., indicated by the red boxes in a and c] and the fit curve by  $A + P\cos(\phi_{RP} + \Phi_{POP})$  (red curve). Two characteristic parameters of the yield oscillation, the contrast P and the phase of the phase  $\Phi_{POP}$ , are indicated in the plot. Since the direction of the SH clock hand is determined by  $2\omega t + \phi_{\rm RP}$ , tuning the relative phase  $\phi_{\rm RP}$  (equivalent to rotating the clock hand) can build a mapping relation between the direction of the FW clock hand,  $\beta_{\omega}(t)$ , with the phase of the phase,  $\Phi_{POP}$ , as illustrated in the left panel of d. When the  $\phi_{RP}$  is tuned to be  $-\Phi_{POP}$ , the two clock hands are parallel and the ionization probability is the maximum.

the phase-of-phase spectroscopy, to resolve the ionization instant of photoelectrons with any momenta on the 46 "detector" and further reconstruct the imaginary tunneling time and the sub-barrier phase acquired in the non-47 stationary tunneling process. A strong elliptically polarized fundamental wave (FW) is used to trigger the dynamical 48 sub-cycle tunneling bursts, and a weak co-rotating circularly polarized second harmonic (SH) serves to perturb 49 the potential barrier uniformly and to probe the time-dependent tunneling dynamics by adjusting the two-color 50 relative phase. The synthesized electric field can be expressed as  $E(t) = [E_{\omega} \cos(\omega t) + E_{2\omega} \cos(2\omega t + \phi_{RP})]\hat{z} + i \epsilon \delta t$ 51  $[\varepsilon E_{\omega}\sin(\omega t) + E_{2\omega}\sin(2\omega t + \phi_{RP})]\hat{x}$ , where  $\varepsilon = 0.80$  is the ellipticity of the FW. The relative phase between the 52 two-color fields  $\phi_{RP}$  was continuously controlled by a pair of fused silica wedges mounted on the piezo-driven 53 motors. The peak intensity of the fundamental field is  $1.0 \times 10^{14} \text{ W/cm}^2$  ( $E_{\omega} = 0.04 \text{ a.u.}$ ; a.u. is atomic unit) 54 and that of the second harmonic was controlled at a very low level about  $1.0 \times 10^{12}$  W/cm<sup>2</sup> ( $E_{2\omega} = 0.004$  a.u.). 55 We measured the photoelectron momentum distribution of single ionization from krypton atoms using cold-target 56 recoil-ion reaction momentum spectroscopy (COLTRIMS)<sup>24,25</sup>. 57

In the fundamental field solely, the photoelectron momentum distribution reveals two lobes, as illustrated in 58 Fig. 1a, which can be understood by angular streaking by elliptically polarized fields (attoclock). The main lobes 59 originate from strong-field tunneling ionization around the two field crests of one optical cycle. The emitting angle 60 of the lobe center deviates from the direction of the laser vector potential at the peak instant, i.e., the x axis. The 61 offset angle is caused by the Coulomb rotation in the continuum<sup>4,5</sup>, while it could be related with the tunneling time 62 delay and exit velocities<sup>6–11</sup>. For all previous attoclock experiments, the offset angle was determined only for the 63 momentum with the maximum yield, and then the angle-to-time mapping was assumed to be isotropic according to 64 the semi-classical model. However, as discussed in this work, for the photoelectron with a general momentum in the 65 final momentum plane, its offset angle is not simply identical to that with the maximum yield since its sub-barrier 66 dynamics is different and its ionization instant will be modified accordingly. Therefore, the construction of the 67 mapping relation between an arbitrary p and t is the critical step to fully characterize the sub-barrier non-stationary 68 tunneling dynamics. 69

In the geometry of POP attoclock, there are two temporal degrees of freedom, i.e., the ionization instant *t* and the two-color relative phase  $\phi_{\text{RP}}$ . The direction of the FW clock hand is uniquely determined by the ionization instant and that of the SH clock hand depends on the two variables. The ionization instant is intrinsic, and we use the externally controllable relative phase to measure the ionization instant. Note that here the calibration of the relative phase does not rely on any theoretical models. At  $\phi_{\text{RP}} = 0$ , the two clock hands both point to the positive direction of z axis at t = 0 (see Figure 1b) and they will be oriented opposite along the *z* axis at the other peak instant  $t = \pi/\omega$ .

Thus, at  $\phi_{RP} = 0$  the left upper electron lobe in the final momentum plane, which corresponds to the peak instant 76 of t = 0, should reach the yield maximum and the right lower lobe should achieve the yield minimum. In Figure 77 1b, we illustrate the angle-integrated energy spectrum for the left upper electron lobe as a function of the relative 78 phase, from which the phase calibration can be performed accurately. After the phase calibration, we illustrate the 79 photoelectron momentum distributions in the two-color fields at the relative phase of zero,  $\pi/6$  and  $\pi/3$  in Figure 80 1c. With the increase of  $\phi_{\rm RP}$ , the centroid of the momentum distribution gradually rotates counterclockwise. In 81 Supplementary Section 3, we illustrate the complete phase-resolved movie of the photoelectron angular distribution. 82 For each momentum [see the example of  $(p_x, p_z, p_y) = (-0.2, 0.74, 0)$  a.u. in Figure 1d], the yield oscillation with 83 respect to the relative phase is close to a standard cosine function  $A + P\cos(\phi_{RP} + \Phi_{POP})$ , where A is the background 84 count, P is the contrast, and  $\Phi_{POP}$  is the so-called phase of the phase<sup>18</sup> ranging from  $-\pi$  to  $\pi$ . Mathematically, the 85 value of  $\Phi_{POP}$  represents the waiting time ( $\Phi_{POP} < 0$ ) or the passed time ( $\Phi_{POP} > 0$ ) of the appearing instant of the 86 yield peak with respect to the instant of  $\phi_{RP} = 0$  during the yield oscillation. However, a clear physical meaning of 87  $\Phi_{POP}$  is not identified in previous phase-of-phase experiments<sup>18–23</sup>. 88

In the phase-of-phase spectroscopy, re-scattering and sub-cycle interference cause the difficulty to dig the deeper 89 physical meaning of the phase of the phase. Here we show it is directly corresponding to the photoelectron ionization 90 instant in this POP attoclock configuration. The photoelectron yield Y at the momentum p exponentially depends 91 on the strength of the synthesized electric field |E(t)| at its ionization instant t. In the POP attoclock, |E(t)| can be 92 reduced to  $F_{\omega}(t) + E_{2\omega}\cos(2\omega t - \beta_{\omega} + \phi_{\rm RP})$ , saving to the first order of the small quantity  $E_{2\omega}/E_{\omega}$ , where  $F_{\omega}(t)$ 93 is the strength of the FW clock hand and  $\beta_{\omega}(t)$  is its orientation angle. Then, one can obtain the momentum- and 94 phase-resolved yield  $Y(\boldsymbol{p}, \phi_{\text{RP}}) \sim \exp[|E(t)|] \sim Y_0(\boldsymbol{p})[1 + E_{2\omega}\cos(2\omega t - \beta_{\omega} + \phi_{\text{RP}})]$  (see Supplementary Section 2 95 for the mathematical derivation), where  $Y_0(\mathbf{p}) \sim \exp[\beta_{\omega}(t)]$  is the yield without adding the perturbative field. Thus, 96 the phase of the yield oscillation with respect to  $\phi_{\text{RP}}$  is  $\Phi_{\text{POP}} = 2\omega t - \beta_{\omega}(t)$ , while the contrast of the yield oscillation 97 is  $Y_0(\mathbf{p})E_{2\omega}$ . For the FW field with high ellipticity, there is  $\beta_{\omega} \approx \omega t$ . Finally, the phase of the phase is directly linked 98 with the ionization instant, i.e.,  $\Phi_{POP} = \omega t$ . 99

The principle of the POP attoclock can be understood intuitively. As illustrated in Figure 1d, varying the relative phase is equivalent to rotating the SH clock hand. When the SH clock hand points to the same direction of the FW clock hand, the photoelectron yield will achieve the maximum and thus this instant is marked. Because the scale of the SH clock has been calibrated, one can use it to measure the direction of the FW clock hand, i.e., the ionization instant.

<sup>105</sup> The experimental phase-of-phase spectrum and the contrast spectrum for krypton atoms are presented in Figure



Figure 2: Experimental results of the POP attoclock. a-b, Measured phase-of-phase spectrum and contrast spectrum for krypton atoms in POP attoclock configuration, respectively. c, The cuts of  $\Phi_{POP}$  along the energies of 4 eV, 8 eV and 16 eV. On the right vertical coordinate the phase of the phase is transformed to the ionization instant using  $\Phi_{POP} = \omega t$ .

2a-b, respectively, which were obtained by Fourier transforming 72 frames of the angle-resolved photoelectron energy 106 spectra with the resolution of  $\Delta \phi_{\rm RP} = \pi/12$ . Here we define the photoelectron emitting angle as  $\theta = \arctan(p_z/p_x)$ , 107 and the momentum  $p_{y}$  along the laser propagation direction was integrated within [-0.1, 0.1] a.u. in the off-line data 108 analysis. When the emitting angle varies 360 degrees, the phase of phase changes  $2\pi$  radians or 360 degrees. This is 109 equivalent to that the photoelectron emitting angle will rotate 360 degrees when varying the relative phase by  $2\pi$ . 110 More importantly, the slope of POP with respect to the photoelectron emitting angle reflects the electron rotation 111 speed in the momentum plane. In Fig. 2c, we illustrate three cuts of the phase-of-phase spectrum along the energies 112 of 4 eV, 8 eV and 16 eV, respectively, and convert  $\Phi_{POP}$  to the ionization instant (see the right vertical coordinate of 113 the plots). The results directly show the mapping relation between the emitting angle and the ionization instant is 114 not angularly uniform, especially for the low-energy photoelectrons. The absolute value of the curve slope is less 115 than 1 when  $\theta$  ranges from 120° to 240° and from  $-60^{\circ}$  to 60°, which indicates the electron rotates slowly when it 116 arrives in the regions of the two main lobes (see Supplementary Section 3 for the animated photoelectron angular 117 distribution). The mapping curve jumps quickly in the low-yield transitional zone between the two main lobes, 118 where the FW clock hand points around the minor axis of the ellipse. For the high-energy electrons, their rotation 119 speed is close to be isotropic. The POP spectrum intuitively shows a dynamical phenomenon that photoelectrons 120 have a angle- and energy-dependent rotation speed even in a circular streaking field, which originates from the 121 non uniform mapping relationship between the emitting angle and the ionization instant. The contrast spectrum is 122 the extent of the response to the weak SH perturbation. Due to the perturbation is isotropic in POP attoclock, the 123 contrast spectrum faithfully reflects the static photoelectron angle distribution in the elliptical FW. 124

To validate our observation and explanation, we first resort to two different tunneling models, the classical 125 trajectory Monte-Carlo (CTMC) simulation<sup>26–28</sup> that is widely used for tunneling from a static barrier, and the 126 strong-field approximation (SFA) model within the saddle-point approach<sup>29</sup> for the non-stationary tunneling. The 127 previous attoclock experiments are mostly explained using the CTMC model<sup>2,3,15</sup>. In the CTMC model, there 128 is neither electron sub-barrier dynamics nor the sub-barrier phase. The potential barrier shape is dictated by the 129 instantaneous strength of the electric field adiabatically. At each ionization instant the tunneled electron burst has a 130 Gaussian distribution centered at zero on the transverse momentum and has no any longitudinal momentum. Thus, 131 the final momentum of the electron burst follows the opposite direction of the laser potential vector at the ionization 132 instant with an additional Coulomb rotation angle. Finally, the photoelectron emission angle is linearly changed 133 with respect to the ionization instant. In the CTMC simulation, we calculated a series of photoelectron momentum 134 distributions at different relative phases and then extracted the phase of the phase with the same procedure for 135

experimental data. The obtained POP spectrum shows that the degree of linearity between the ionization instant and the emitting angle is pretty good (i.e., the slopes of the mapping curves in Fig. 3b are all close to -1). The left-right shift between these mapping curves can be attributed to the Coulomb rotation. In SI, we present the CTMC result without including the Coulomb potential and the obtained mapping curves are all overlapped. Thus, previous attoclok experiments that were interpreted with the CTMC model is not very accurate because the sub-barrrier effect is not seriously included.

By contrast, the non-stationary tunneling model (SFA) includes a time-dependent tunneling process on the 142 imaginary time axis (see Fig. 4a). For the quantum path of each final momentum p, its ionization time, i.e., the saddle 143 point  $t_s(\mathbf{p}) = t_r(\mathbf{p}) + t_i(\mathbf{p})$ i, is a complex number governed by the saddle-point equation  $[\mathbf{p} + \mathbf{A}(t_s)]^2/2 + I_p = 0$ . The 144 real part of the ionization time,  $t_r$ , represents the emitting instant from the barrier, which is the measured phase of 145 the phase in this work. The imaginary part of the ionization time,  $t_i$ , is the so-called Keldysh tunneling time<sup>30</sup>, which 146 decides the duration time of the tunneling along the imaginary time axis. During the tunneling, i.e., progressing from 147  $t_s$  to  $t_r$ , the electron accumulates a time-dependent complex action  $S[t_r(\mathbf{p})] = \int_{t_s}^{t_r} [\mathbf{p} + \mathbf{A}(t)]^2 / 2 + I_p dt$ . The imaginary 148 part of the action at the tunnel exit is associated with the probability of the quantum path by the exponential 149 factor  $\exp(-2Im[S])$ , which corresponds to the measured contrast in POP attoclock. The real part of the action is 150 the sub-barrier phase, which governs the initial phase of electron wave function in the continuum (see Fig. 4b). 151 The laser field will excite the tunneling electron under the barrier and thus the quantum path model predicts a 152 center-shifted Gaussian-like distribution for the transverse momentum and a nonzero time-dependent distribution 153 for the longitudinal momentum at the exit<sup>13,31,32</sup>. These non-stationary tunneling features will destroy the uniform 154  $\theta - t_r$  mapping relation in the CTMC model. In SI, we illustrate the time-resolved distributions of the exit velocities 155 from SFA and use them as the initial condition for the CTMC simulation. The obtained POP spectrum emerges the 156 non-uniform mapping. More discussions about the relation and difference between the static and the non-stationary 157 tunneling models are presented in the theoretical part of Methods. 158

In Fig. 3c, we show the momentum-resolved distribution of  $t_r$ , which is obtained directly by solving the saddlepoint equation *in the fundamental field*. The saddle-point result agrees with the experiment and the energy-dependent mapping relations between  $\theta$  and  $t_r$  are well reproduced. Therefore, this POP-attoclock could reveal the features of the non-stationary tunneling, which are usually hidden in static photoelectron spectra of attoclock with one-color elliptically or circularly polarized fields. In Supplementary Figure 5, we present the extracted phase of phase spectrum using POP attoclock from calculated photoelectron momentum distributions by numerically integrating the transition matrix element of SFA, following the experimental and CTMC procedure. The extracted result



Figure 3: **Calculated phase-of-phase spectra**. **a,b**, The spectra of  $\Phi_{POP}$  and the corresponding cuts along different energies from the CTMC simulation. **c,d**, The distribution of the real part of the saddle point and its corresponding cuts based on the SFA model. **e,f**, The results of the CCSFA simulation. **g,h**,The results of the TDSE simulation. The isolines of  $\Phi_{POP}$  or  $t_r = 1.0$ , 0, and -1.0 radian are plotted in a,b,e, and g.

agrees very well with the saddle-point result, which self-consistently proves that the POP attoclock can measure the 166 ionization instant. In circular or elliptical light fields, one needs to consider the influence of the magnetic quantum 167 number of the ground state of atoms, since the  $p_+$  and  $p_-$  orbitals will display the ionization dichroism in static 168 photoelectron energy spectra<sup>33,34</sup>. The magnetic quantum number will affect the probability of electron trajectories 169 via the pre-exponential factor of the transition matrix element but has no effect on the saddle point. Therefore, the 170 POP spectrum is less sensitive to the magnetic quantum number, and on the contrary the contrast spectrum will 171 show the same ionization dichroism features as the static photoelectron energy spectrum (see Supplementary Figure 172 4). To reveal the dependence of the POP spectrum on the nonadiabaticity of tunneling, in Supplementary Figure 173 6 we present the calculated POP spectra at other two wavelengths (1200 nm and 1800 nm) for the FW from the 174 SFA model. The result demonstrates that the non-uniform mapping gradually disappears with the increase of laser 175 wavelength or the nonadiabaticity of tunneling. 176

In all attoclock experiments, the rotation of the long-range Coulomb potential by elliptical or circular fields will 177 modify the electron momentum after tunneling, and mainly causes the offset angle in the final momentum plane. To 178 investigate the effect of the Coulomb potential on the POP spectrum, we have further performed the calculation 179 with the Coulomb-corrected strong-field model<sup>35–37</sup> (CCSFA) and the numerical solution of the time-dependent 180 Schrödinger equation<sup>38</sup> (TDSE) (see Methods for the details). The CCSFA model is based on SFA and the effect of 181 the long-range Coulomb potential has been included. The TDSE results can be viewed as the benchmark for all the 182 models. From the results of these two models, the POP spectrum will be shift by the offset angle, as indicated by the 183 ioslines in Fig. 3e-g. Both models show the low-energy electrons will be more affected by the Coulomb rotation. 184 Although the Coulomb rotation will shift the POP spectrum left to some extent, basically it does not alter the slope of 185 the POP curves (see the CTMC result in Fig. 3a-b), which reflects the sub-barrier non-stationary tunneling dynamics. 186

Importantly, the tunneling process not only modifies the amplitude of the electron wavepacket (i.e., initial 187 momentum distributions), but also imprints a remarkable phase on it. The POP attoclock enables us to obtain the 188 electron sub-barrier phase information. This approach does not need the interference pattern on photoelectron 189 momentum distribution<sup>39</sup>. With the measured phase of the phase and the contrast, we can further reconstruct the 190 other two quantities of the imaginary-time tunneling picture,  $t_i$  and Re[S], according to the sub-barrier integration 191 equation of the action. Our reconstruction approach is very straightforward and robust, which has been justified 192 using the input of  $t_r$  and Im[S] extracted from the photoelectron momentum spectra of SFA (see Supplementary 193 Figure 5). To isolate the sub-barrier dynamics from the classical dynamics in the continuum, one needs to subtract 194 the Coulomb rotation angle from the measured photoelectron emission angle, being consistent with the SFA model. 195



Figure 4: **Sub-barrier tunneling dynamics. a**, Tunneling picture and the reconstruction of  $t_i$  and Re[S]. **b**, Illustrations for the phase evolution at three ionization instants. The sub-barrier phase indicated by Re[S] at the tunnel exit, is dependent on the dynamical change of the barrier. **c-d**, The final-momentum-resolved distribution of the imaginary tunneling time  $t_i$  and the sub-barrier phase Re[S], respectively, which are obtained by solving the saddle-point equation and the integration equation of the action. **e-f**, The reconstructed distributions of  $t_i$  and Re[S] using the measured phase-of-phase spectrum and the contrast spectrum, respectively.

The reconstructed results from experiments (Fig. 4e-f) agree well with the theoretical results of the quantum path approach (Fig. 4c-d), revealing a clear time- and energy-dependent sub-barrier feature on the distributions.

For the imaginary tunneling time  $t_i$ , it reflects the static property of the potential barrier, i.e., the barrier thickness 198 decided by the instantaneous strength of the electric field. The imaginary tunneling time will reach the minimum ( $\sim$ 199 500 attoseconds) when the electric field vector points to the major axis of the ellipse (i.e., the emitting angle  $\theta = 180^{\circ}$ ) 200 and it will increase to 800 attoseconds when the polarization vector points to the minor axis. The energy dependence 201 of  $t_i$  is also important, which controls the radial spread of the photoelectron momentum distribution. Under the 202 adiabatic approximation [E(t) = E, A(t) = -Et], the imaginary tunneling time can be obtained analytically as 203  $t_i = \sqrt{(2I_p)/E}$ , and it has no any energy dependence. The corresponding ionization rate exp(-2ImS) becomes 204 back to the ADK rate<sup>40</sup> used in CTMC (i.e.,  $\exp[-2(2I_p)^{3/2}/(3E)]$ ), which shows a narrower radial spread of the 205 photoelectron momentum distribution compared with the non-adiabatic case<sup>13,14</sup>. 206

In contrast to the imaginary tunneling time, the sub-barrier phase reflects the dynamical properties of the quickly 207 changing Coulomb barrier, i.e, the derivative versus time. When the electric field vector points to the major or 208 minor axis of the ellipse, the barrier is stationary and thus the electron doesn't acquire any phase in agreement with 209 the Wentzel-Kramers-Brillouin approximation solution (real number) under the barrier<sup>41</sup>. When the electric field 210 vector deviates the stationary instants, the electron acquires a sub-barrier phase whose sign is dependent on the 211 change direction of the barrier, i.e., the barrier thickness is increasing or decreasing. In Fig. 4b, we illustrate the 212 phase evolution at three ionization instants at the rising edge, stationary point, and falling edge of the light electric 213 field, respectively. This clearly proves the sub-barrier phase is dependent on the dynamical change of the barrier. 214 Moreover, both experiment and theory indicate that the low-energy component of the tunneling wave function has 215 a more prominent sub-barrier phase, as there the sub-barrier interaction time and length are larger. Note that the 216 POP attoclock can provide the time- and energy-resolved dynamical information about tunneling compared with the 217 common static attoclock scheme. 218

In conclusion, we have calibrated the attoclock with the two-color phase-of-phase photoelectron spectroscopy, and employed this POP attoclock to build the accurate angular streaking relationship between an arbitrary final momentum and its ionization instant in the full momentum space. The results demonstrate the widely-used angular streaking capability of light fields is not angularly homogeneous and the ionization instants along the same emitting angle have a strong energy dependence, which both contradict with the static tunneling model. Using the measured ionization instant and ionization probability, we have reconstructed the imaginary tunneling time and the electron sub-barrier phase, which contains the static and dynamical information of the tunneling process, serving as a complete characterization of sub-barrier tunneling dynamics in strong-field ionization. Based on this work, the POP
 attoclock has the appealing potential application in the attosecond metrology of the oriented molecules, crystal solids
 and liquids<sup>42</sup>.

#### 229 Methods

**Experimental details.** Supplementary figure 1 schematically shows the experimental setup for phase-of-phase 230 attoclock. The *p*-polarization fundamental light field pulses were delivered from a multipass Ti:sapphire amplifier at 231 a central wavelength of 800 nm with the repetition rate of 3 kHz. The pulse duration is 25 fs with full width of half 232 maximum in intensity. The second harmonic pulses at the central wavelength of 400 nm were produced by frequency 233 doubling with a 200- $\mu$ m-thick type-I beta-barium borate (BBO) crystal (29.2° cut). Then, the two light fields were 234 synchronized in a Mach-Zehnder interferometer scheme with 5-attosecond precision and their polarizations and 235 intensities were controlled, independently. In each arm of the interferometer, the intensity and polarization of the 236 light field were monitored by a wire grid polarizer and half-wave and quarter-wave retardation plates, respectively. 237 The fundamental field was adjusted to be the elliptical polarization whose major axis was fixed along the z axis and 238 the second harmonic field was tuned to a co-rotating circular polarization in the same polarization plane (x-z plane). 239 The light beam was focused by a silver-coated concave mirror with focal length f = 75 mm, which was placed inside 240 the high-vacuum chamber ( $< 10^{-10}$  mbar) of the COLTRIMS set-up. The supersonic gas jet of krypton atoms (2 241 Bar) was delivered along the x direction by a small nozzle with a opening hole diameter of 30  $\mu m$ . In COLTRIMS, 242 static electric ( $\sim 3.2$  V/cm) and magnetic ( $\sim 5.4$  G) fields were applied along the z axis to collect the charged 243 fragments in coincidence. Only the single ionization (one electron is coincident with one  $kr^+$ ) events are presented 244 in this work. 245

**CTMC simulation.** In the CTMC model, the tunnelled electrons have a Gaussian distribution on the transverse mo-246 mentum  $(v_{\perp})$  perpendicular to the instantaneous laser field and zero longitudinal momentum along the instantaneous 247 laser field direction. Each electron trajectory is weighted by the ADK ionization rate  $W(t, v_{\perp}^{i}) = W_{0}(t)W_{1}(v_{\perp}^{i})^{27,28}$ , 248 in which  $W_0(t) = |(2I_p)^2/E(t)|^{2/\sqrt{2I_p}-1} \exp[-2(2I_p)^{3/2}/|3E(t)|]$  determines the ionization rate with respect to the 249 ionization instant, and  $W_1(v_{\perp}^i) = \sqrt{2I_p}/E(t)\exp[-\sqrt{2I_p}(v_{\perp}^i)^2/|E(t)|]$  determines the initial transverse momentum 250 distribution, where E(t) is the instantaneous strength of laser field and  $I_p$  is the ionization potential. The electron 251 tunneling exit is along the instantaneous direction of the synthesized light field and its value is given by  $I_p/|E(t)|$ . 252 After sampling all the electrons, their classical motion outside the barrier is governed by the Newtonian equation 253  $\ddot{\mathbf{r}} = -E(t) - \mathbf{r}/r^3$  until the laser is turned off, where r is the distance from the electron to the nucleus. In the 254 simulation, we use a sin<sup>2</sup>-shape pulse envelope with the duration of 12 cycles for the SH field. At the end of the 255

laser pulse, we select the electrons with positive energy and record their positions and their momenta. The electron asymptotic momenta on the virtual detector are transformed according to the Kepler's laws. Finally, we statistic the electron trajectories using the 200×200 bins in the momentum regime of  $p_x \times p_z$ = [-1.5,1.5]a.u.×[-1.5,1.5]a.u.. We totally calculate 24 frames of the photoelectron momentum distributions for the two-color relative phase distributing from 0 to  $2\pi$  uniformly. The calculated phase-resolved photoelectron momentum distributions are presented in SI, from which we use Fourier transform to obtain the phase-of-phase spectrum shown in Fig. 3a.

Strong-field approximation model. In the strong-field approximation, the final-momentum-resolved ionization 262 matrix element is given by  $M_p = -i \int_0^{t_f} \langle \boldsymbol{p} + \boldsymbol{A}(\tau) | \boldsymbol{r} \cdot \boldsymbol{E}(\tau) | \psi_{\text{initial}} \rangle \exp(iS(\tau)) d\tau$ , where  $S(\tau) = \int_0^{\tau} [\boldsymbol{p} + \boldsymbol{A}(\tau)]^2 / 2 + C(\tau) | \psi_{\text{initial}} \rangle \exp(iS(\tau)) d\tau$ . 263  $I_p dt$ ,  $t_f$  is the laser turn-off time, and  $\psi_{\text{initial}}$  is the initial wavefunction of electrons. In the calculation, we adopt 264 the asymptotic form of the hydrogenlike atomic wavefunction  $\psi_{\text{initial}} = \exp(-\sqrt{(2I_p)r})Y_{1m}(\theta,\phi)/r$  as the initial 265 wavefunction of Kr atoms, where m = 1 and -1 represent the  $p_+$  and  $p_-$  orbitals, respectively. By the numerically 266 integrating the ionization matrix element, we obtained the phase-resolved photoelectron momentum distributions 267 from  $p_+$  and  $p_-$  orbitals, respectively. From the photoelectron momentum spectra, we extracted the phase-of-phase 268 spectrum. Note that using the saddle-point method one can avoid the numerical integration and introduce the 269 concept of the quantum path. The saddle point  $t_s(\mathbf{p})$  is determined by the equation  $[\mathbf{p} + \mathbf{A}(t_s)]^2/2 + I_p = 0$ , which 270 is solved by a complex root finding routine. In the elliptical light field, one final momentum can correspond to 271 two saddle points and only one of them is physical. By judging the ionization probability of the quantum path, 272 one can select the physical one. During tunneling (i.e., from  $t_s$  to  $t_r$ ), the electron acquires a complex action 273  $S(t_r) = \int_{t_s}^{t_r} [\mathbf{p} + \mathbf{A}(\tau)]^2 / 2 + I_p d\tau$ . The real part of the action is the sub-barrier phase and the imaginary part governs 274 the ionization rate by  $W = \exp(-2\text{Im}[S(t_r)])$ . In the main text, we show  $t_r$ ,  $t_i$  and Re[S], which are obtained by 275 directly solving the saddle-point equation and propagates the quantum path under the barrier. On the other hand, we 276 present the corresponding results in SI, which are obtained by the extraction method of POP attoclock. They agree 277 very well with each other, which strongly verified the reliability of POP attoclock. Note that in the adiabatic limit 278 [E(t) = E, A(t) = -Et], there is  $t_i = \sqrt{(v_{\perp} + 2I_p)/E}$  and thus the exponential factor of the ionization rate can be 279 evaluated as  $W = \exp[-2(2I_p)^{3/2}/(3E)]\exp[-\sqrt{2I_p}(v_{\perp})^2/E]$ , which is exactly the ADK rate used in the adiabatic 280 CTMC model. 281

**Coulomb-corrected strong-field approximation simulation.** The CCSFA model is based on the saddle-point approach of the SFA. We randomly sample 10<sup>7</sup> points in the final momentum plane ( $p_x$ ,  $p_z = [-1.5, 1.5]$  a.u.). After determining the ionization time of each quantum path by the saddle-point equation in the two-color field, we then propagate these electron trajectories with real variables using Newton's equation  $\ddot{\mathbf{r}} = -E(t) - \mathbf{r}/r^3$  to simulate the electron dynamics outside the barrier. The weight of the electron trajectories is given by  $W = \exp(-2\text{Im}[S(t_r)])$ without considering the pre-exponential factor. The electron tunnel exit position and exit momentum are determined by the imaginary-time propagation under the barrier, i.e.,  $\mathbf{r}_{exit} = \int_{t_s}^{t_r} [\mathbf{p} + \mathbf{A}(t)] dt$  and  $\mathbf{p}_{exit} = \mathbf{p} + \mathbf{A}(t_r)$ . After the laser pulse turns off, we obtain the electron asymptotic momenta on the virtual detector according to the Kepler's laws. Then we obtain the photoelectron momentum distribution on the "detector" using the same method as CTMC.

**TDSE simulation.** Details of the algorithm and the source code are in the publication<sup>38</sup>. Briefly, we first obtain the 291 atomic initial-state wave-function through the imaginary time propagation method. In the simulation we use the 292 effective model potential  $V_{eff} = -[Z + (Z_{full} - Z)\exp(-r_s \cdot r)]/r$ , where Z = 1 and  $Z_{full} = 36$  are the asymptotic 293 ion charges as  $r \to \infty$  and  $r \to 0$ , respectively. The screening length  $r_s = 7.7631$  is used to match the ionization 294 potential  $I_p = -14.0$  eV for krypton atom. The initial magnetic quantum number m can be tuned to 1, 0 and -1 295 without changing the ionization potential. The laser parameters are identical in all simulations shown in the main 296 text. Secondly, we perform the real-time evolution of the wave-function in the laser and the Coulomb combined 297 field within the dipole approximation. The wave-function is expanded in spherical harmonics, and time-propagation 298 is performed using a split-operator approach. Finally, when the laser turns off, the photoelectron momentum 299 distribution is evaluated with a time-dependent surface flux method. The calculated phase-resolved movie of 300 photoelectron momentum distributions is shown in SI. From these photoelectron momentum distributions we extract 301 the POP spectrum shown in Fig. 3g. 302

**Reconstruction of**  $t_i$  and Im[S]. Using the expression of the laser field, one can derive the real part and imaginary part of the electron sub-barrier action analytically, as given by,

$$Re[S] = -p_z E_{\omega} / \omega^2 \cos \omega t_r (1 - \cosh \omega t_i) - p_x \varepsilon E_{\omega} / \omega^2 \sin \omega t_r (1 - \cosh \omega t_i) + (1 - \varepsilon^2) E_{\omega}^2 / (8\omega^3) \sin 2\omega t_r (1 - \cosh 2\omega t_i).$$
(1)

$$Im[S] = (p^2/2 + I_p + U_p)t_i - p_z E_\omega / \omega^2 \sin \omega t_r \sinh \omega t_i + p_x \varepsilon E_\omega / \omega^2 \cos \omega t_r \sinh \omega t_i - (1 - \varepsilon^2) E_\omega^2 / (8\omega^3) \cos 2\omega t_r (\sinh 2\omega t_i).$$
(2)

The phase-of-phase spectrum directly reflects the distribution of  $t_r$ , and the contrast spectrum is corresponding to exp(-2Im[S]), which is normalized to the maximum of the theoretical distribution in the reconstruction process. Using the measured spectra of  $t_r$  and exp(-2Im[S]), we start from Equation 2 to evaluate  $t_i$  by the numerical method of solving the non-linear equation for each final momentum. Then using the measured  $t_r$  and the reconstructed  $t_i$ , through Equation 1 we can obtain Re[S], i.e., the sub-barrier phase. Note that we have reduced the classical Coulomb rotating effect in experiment. The electron emitting angle  $\theta$  was shifted to cancel the offset angle in reconstruction process, which is in consistence with the SFA model.

#### **310 Data availability**

The data that support the plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

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#### **Author contributions statement**

M. H., P. G., and Z. G. performed the experiments. M. H., Y. F. and Y. L. analyzed and interpreted the data. Simulations were implemented by M. H.. This project was coordinated by Y. L.. All authors discussed the results and wrote the paper.

#### **409** Competing interests

410 The authors declare no competing interests

#### **Additional information**

Supplementary information is available for this paper. Correspondence and requests for materials should be addressed
to Y. L..